

**UNIVERSITY OF CALIFORNIA**  
**College of Engineering**  
**Department of Electrical Engineering and Computer Sciences**

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**Midterm**  
**Thursday, March 8, 2012**

**EECS 240**  
**SPRING 2012**

*You should write your results on the exam sheets only. Partial credit will be given only if you show your work and reasoning clearly.*

*Throughout the exam, you can ignore flicker noise, assume that the  $r_o$  of the transistors is infinite, and ignore all capacitors except those drawn in the circuit unless the problem states otherwise.*

**Name:** \_\_\_\_\_

**SID:** \_\_\_\_\_

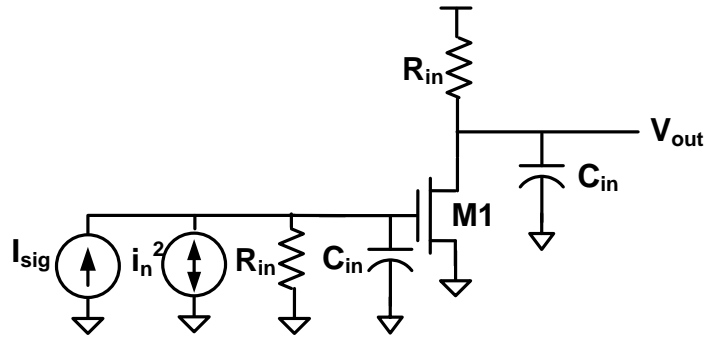
**Problem 1** \_\_\_\_\_ / 16

**Problem 2** \_\_\_\_\_ / 12

**Problem 3** \_\_\_\_\_ / 12

**Total** \_\_\_\_\_ / 40

**Problem 1 (16 points) Noise and SNR**



In this problem we will be examining the circuit shown above, where  $I_{sig}$  is a sinusoidal input current with an amplitude of  $A_I$  and angular frequency  $\omega$ , and  $i_n^2$  is a white noise current source with a power spectral density of  $4kT/R_n$ .

- a) (4 pts) What is the s-domain transfer function that both  $I_{sig}$  and the noise current  $i_n^2$  experience to arrive at  $V_{out}$ ? You can assume that the transistor M1 is biased in saturation with a given  $g_m$ .

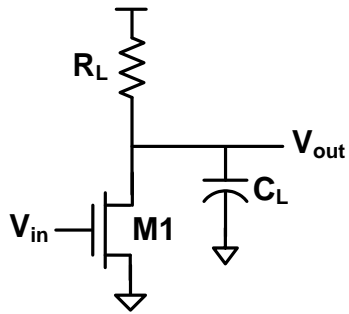
- b) (4 pts) Given your answer to part a), what is the voltage noise variance at  $V_{out}$  due to  $i_n^2$  ( i.e.,  $V_{out}^2(i_n)$  )? You should provide your answer in terms of  $R_{in}$ ,  $C_{in}$ ,  $g_m$ ,  $R_n$ , and  $kT$ .

- c) **(8 pts)** What are the mean-squared signal voltage ( i.e.,  $V_{\text{out}}^2(I_{\text{sig}})$  ) and the SNR ( i.e.,  $V_{\text{out}}^2(I_{\text{sig}})/V_{\text{out}}^2(i_{\text{n}})$  ) at  $V_{\text{out}}$ ? Note that you can ignore any noise from the transistors/resistors, and that you should provide your answer in terms of  $\omega$ ,  $A_I$ , and the same quantities as part b).

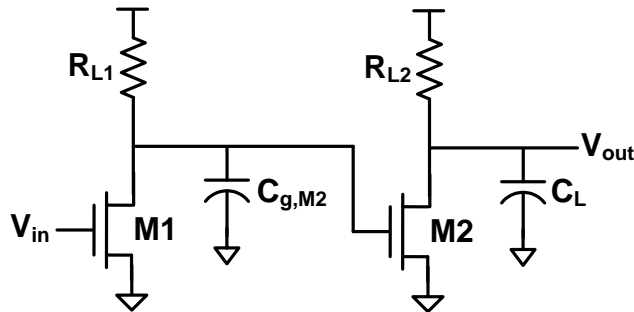
- d) **(BONUS)** If we express  $R_{in}C_{in}$  as  $K_{bw}/\omega$ , what choice of  $K_{bw}$  would result in the maximum SNR for this circuit?

## Problem 2 (12 points) Amplifier Power

- a) (4 pts) How much bias current is required for the amplifier shown below to achieve a gain of  $A_v$  and bandwidth of  $\omega_{bw}$ ? You should provide your answer in terms of  $A_v$ ,  $\omega_{bw}$ ,  $C_L$ , and the  $V^*$  of M1.



- b) **(8 pts)** Now let's see what happens if we try to achieve the same total gain  $A_v$  and bandwidth  $\omega_{bw}$  using the two stage design show below. For simplicity, let's assume that we will make the gains and bandwidths of each individual amplifier stage identical, that the  $V^*$ 's of M1 and M2 are identical, and that the bandwidth of a circuit with two poles at  $\omega_p$  is  $\omega_p/2$  (i.e., the overall bandwidth of the two stage amplifier is half the bandwidth of each individual stage). Under these conditions, how much total bias current ( $I_{M1} + I_{M2}$ ) is required to achieve the same total gain and bandwidth? You should provide your answer in terms of the  $\omega_T$  ( $=g_m/C_g$ ) of the transistors and the same parameters as part a).

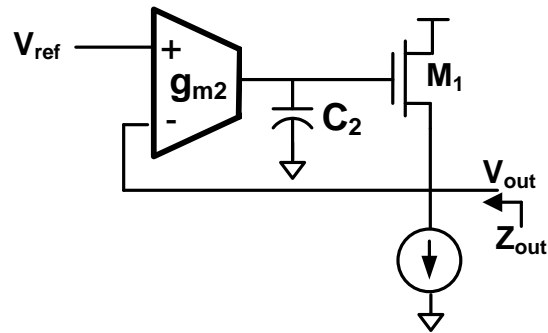


c) **(BONUS)** Under what condition will the two-stage design from part b) require less bias current than the single stage design from a)?



### Problem 3 (12 points) Voltage Source Design

In this problem we will examine how to use the structure shown below (which happens to bear some resemblance to a gain-boosted cascode) in order to build a voltage source with a low output impedance. Note that you can assume that the OTA ( $g_{m2}$ ) is ideal.



- a) (6 pts) As a function of  $g_{m1}$ ,  $g_{m2}$ , and  $C_2$ , what is the s-domain output impedance  $Z_{out}(s)$  of the circuit shown above?

- b) **(6 pts)** Assuming that  $g_{m1} = 10\text{mS}$  and that we would like to make sure that at 100MHz the magnitude of the output impedance (i.e.,  $\|Z_{out}(j*2\pi*100\text{MHz})\|$ ) is less than  $10\Omega$ , what is the minimum gain-bandwidth (i.e.,  $g_{m2}/C_2$ ) required of the OTA in part a)? You should provide your answer in Hz.