

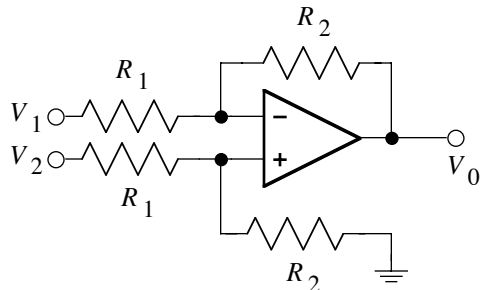
UNIVERSITY OF CALIFORNIA, BERKELEY  
 Electrical Engineering and Computer Sciences Department

EECS 145L Electronic Transducer Lab  
 MIDTERM #1 (100 points maximum)  
 September 30, 2002

(closed book, calculators OK, equation sheet provided)  
 (You will not receive full credit if you do not show your work)

**PROBLEM 1 (35 points)**

Consider the differential amplifier circuit shown below:



**Assume the following:**

- The op-amp open loop gain is infinite
- The op-amp input impedances are infinite.

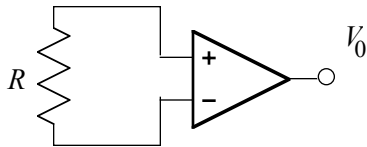
**Do the following:**

**1a** (25 points) derive the equation for the differential gain as a function of the resistor values  $R_1$  and  $R_2$

**1b** (10 points) derive the equation for the common mode gain as a function of the resistor values  $R_1$  and  $R_2$

**PROBLEM 2 (30 points)**

In this problem you will consider an instrumentation amplifier as used to measure the rms Johnson noise in a resistor  $R$ .



The instrumentation amplifier has the following characteristics:

- Amplifier noise rms (relative to input) =  $12.9 \text{ nV Hz}^{-1/2} \text{ sqrt}(\Delta f)$
- Gain-bandwidth product = 100 MHz
- Input leakage currents can be neglected
- The gain can be set by external resistors (since these resistors are after the first gain stage, you can neglect their Johnson noise)

**2a** (5 points) With the instrumentation amplifier set for a differential gain of 100, and  $R = 1 \text{ M}\Omega$  at  $T = 300 \text{ K}$ , what is the total rms noise voltage (amplifier plus resistor) at the amplifier output ?  
Hint: See the equation sheet for Johnson noise and combining random variables

**2b** (5 points) With the instrumentation amplifier set for a differential gain of 10,000, and  $R = 1 \text{ M}\Omega$  at  $T = 300 \text{ K}$ , what is the total rms noise voltage at the amplifier output?

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**2 c** (5 points) With the instrumentation amplifier set for a differential gain of 10,000, and  $R = 1 \text{ M}\Omega$  at  $T = 75 \text{ K}$ , what is the total rms noise voltage at the amplifier output?

**2 d** (5 points) With the instrumentation amplifier set for a differential gain of 10,000, and  $R = 500 \text{ k}\Omega$  at  $T = 300 \text{ K}$ , what is the total rms noise voltage at the amplifier output ?

**2 e** (5 points) With the instrumentation amplifier set for a differential gain of 10,000,  $R =$  two  $500 \text{ k}\Omega$  resistors in series, use the result from part 2d to compute the total rms noise voltage at the amplifier output. (Hint: use the formula for adding two independent random variables)

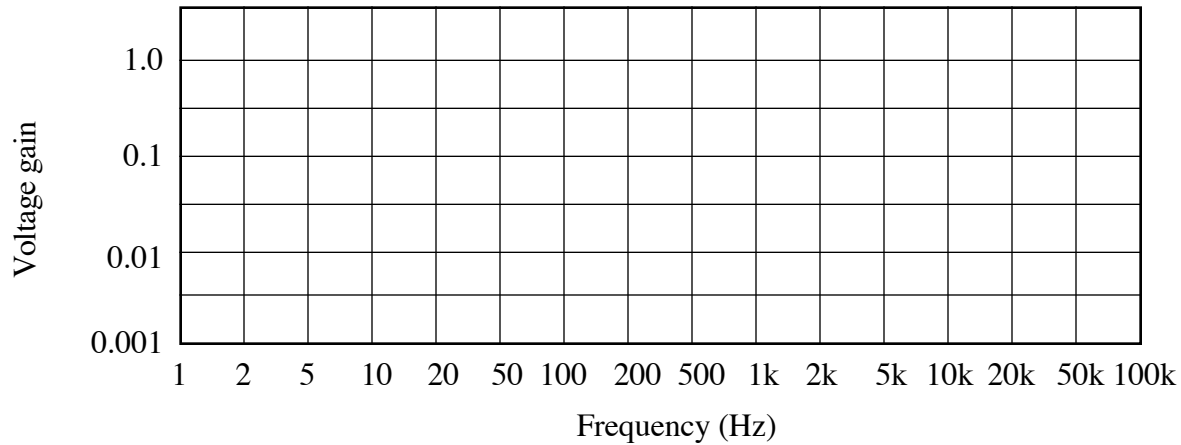
**2 f** (5 points) With the instrumentation amplifier set for a differential gain of 10,000, and  $R = 1 \text{ M}\Omega$ , at what resistor temperature  $T$  does its Johnson noise equal the instrumentation amplifier noise?

**PROBLEM 3 (35 points)**

Design an analog filter circuit that has the following properties

- Gain between 0.9 and 1.0 for frequencies between 100 Hz and 20 kHz
- Gain less than 0.001 for frequencies above 52 kHz
- Gain less than 0.01 at 60 Hz
- Gain less than 0.001 for frequencies below 2 Hz

**2a** (10 points) Sketch the required gain vs. frequency below



**2b** (25 points) Design a filtering circuit that meets the requirements above with the minimum complexity and cost. **For each filtering element, give type, corner frequency, and order number.** (Hint: see equation sheet for a table of  $f/f_c$  vs. gain and order.) Do not give resistor and capacitor values.