## EECS 120

## FINAL EXAM

Friday, May 17, 1996, 5:00-8:00 p.m.

Name: $\qquad$ ID\#: $\qquad$

- Closed book. Three sides of notes. No calculators.
- There are 8 problems worth 200 points total. The problems on this exam may have several solution methods. One method may be much more time efficient compared to the others. Points are proportional to amount of time problem may take, using an efficient approach.

| Problem | Points | Your Score | Problem | Points | Your Score |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20 |  | 6 | 25 |  |
| 2 | 10 |  | 7 | 35 |  |
| 3 | 30 |  | 8 | 30 |  |
| 4 | 25 |  |  |  |  |
| 5 | 25 |  |  |  |  |
| Total | 110 |  |  | 90 |  |

In the real world, unethical actions by engineers can cost money, careers, and lives. The penalty for unethical actions on this exam will be a grade of zero and a letter will be written for your file and the Office of Student Conduct.

Problem 1 (20 points)
Classify the following systems. In each column, write "yes", "no", or "?" (use "?" if not decidable with given information). The input to the system is $x(t)$ and output is $y(t)$. (To discourage random guessing, +1 for correct, 0 for blank, $-\frac{1}{2}$ for incorrect.)

| System |  |  | Time- <br> invariant | BIBO <br> stable |
| :--- | :--- | :--- | :--- | :--- |
| a. $y(t)=x(t)+u(t-1)$ |  |  |  |  |
| b. $y(t)=\int_{-\infty}^{t} \sqrt{\|x(\tau)\|} d \tau$ |  |  |  |  |
| c. $y(t)=x(t) *\left(\sin \left(\omega_{0} t\right) u(t)\right)$ |  |  |  |  |
| d. $y(t)=\int_{-\infty}^{t+1} x(\tau) d \tau$ |  |  |  |  |
| e. $y(t)=x(t)+\int_{-\infty}^{\infty} x(\tau)\left[e^{-(t-\tau)} u(t-\tau)\right] d \tau$ |  |  |  |  |

## Problem 2 (10 points)

Sketch the following time functions, labelling maximum amplitude.
[2 pts.] a) $\cos (2000 \pi t)$

[2 pts.] b) $\cos (2000 \pi t+\pi / 2)$

[6 pts.] c) $(1+\cos (200 \pi t)) \cos 2000 \pi t$


## Problem 3 ( 30 points)

Consider a periodic signal $m(t)$ shown below:

[12 pts.] a) Sketch $M(\omega)$, labelling heights, center frequency, and spacing.

[10 pts.] b) Let $x(t)=(1+0.5 m(t)) \cos \omega_{c} t$, with $\omega_{c}=200 \pi$. Sketch $X(\omega)$, labelling heights, center frequencies, and spacing.

[2 pts.] c) What kind of modulation technique is used to generate $x(t)$ ? (Circle one.)
AM DSB — with carrier upper sideband
AM DSB — no carrier lower sideband
wideband frequency modulation
wideband phase modulation
interrupted continuous wave narrowband frequency modulation narrowband phase modulation
[4 pts.] d) What is the ratio of power in the sidebands to power in the carrier for $x(t)$ ?
[2 pts.] e) Explain (assuming knowledge of EE40) what modulation is good for and why it is used in communications systems.

Consider the causal system shown in the block diagram below, with input $x(t)$ and output $y(t)$ :

[7 pts.] a) Find the transfer function for the system.

$$
H(s)=\frac{Y(s)}{X(s)}=\square
$$

[6 pts.] b) With $k_{1}=0, k_{2}=0$, what is the impulse response for the system? Is the system BIBO stable? Why or why not?

$$
h(t)=\square
$$

[6 pts.] c) Find values of $k_{1}$ and $k_{2}$ such that the closed loop system has 2 poles at $s=-4$.

$$
\begin{array}{|l|}
k_{1}=
\end{array} k_{2}=
$$

[6 pts.] d) For positive $k_{2}$, what is the minimum value of $k_{1}$ for the closed loop system to be BIBO stable?

$$
k_{1}>
$$

Consider the following difference equation:

$$
y[n]-\frac{3}{4} y[n-1]+\frac{1}{8} y[n-2]=5 x[n]
$$

[5 pts.] a) For $x[n]=\delta[n-1]$, what is the zero state response?

$$
y_{\mathrm{ZSR}}[n]=
$$

[5 pts.] b) Assuming $y[-1]=1$ and $y[-2]=2$, what is the zero input response?

$$
y_{\mathrm{ZIR}}[n]=
$$

[5 pts.] c) Is the system BIBO stable? Why or why not?
[5 pts.] d) What is $\lim _{n \rightarrow \infty} y[n]$ if $x[n]=3 u[n]$ ?

$$
\lim _{n \rightarrow \infty} y[n]=
$$

[5 pts.] e) Assuming zero initial conditions, what is the steady state response to $x[n]=e^{j \pi n}$ ?

$$
y[n]=
$$

A continuous time filter has impulse response

$$
\imath(t)=\left(e^{-t}-e^{-.5 t}\right) u(t)
$$

[10 pts.] a) Find the corresponding digital filter $H(z)$ using impulse invariant techniques and sample time $T=0.5 \mathrm{sec}$ where $\left(e^{-.5} \approx .61\right.$ and $\left.e^{-.25} \approx .78\right)$.

$$
H(z)=
$$

[15 pts.] b) Sketch $\left|H\left(e^{j \omega T}\right)\right|$ in range $\frac{-4 \pi}{T}<\omega<\frac{4 \pi}{T}$, labelling maximum and minimum amplitude. (Maximum and minimum may be left as functions of $e^{x}$ ). $T=0.5 \mathrm{sec}$.


A system is described by the following block diagram:

[30 pts.] a) Let $x(t)=\cos 4 \pi t$. Sketch $X^{\prime}(\omega)$ and $\tilde{X}(\omega)$, labelling peak magnitude, zero crossing(s), and spacing. (Hint: $X^{\prime}(\omega)$ and $\tilde{X}(\omega)$ should be real.)

[5 pts.] b) What is the relationship between $\tilde{X}(\omega)$ and the 10 point DFT of $x[n]=X[k]$ (where $x[n]=x(0) \ldots x(.9))$ ? Explain why. (What is the effect of not shifting the window $w(t)$ by T/2?)

For each pole-zero diagram below, fill in the box with the letter of the corresponding frequency response and unit sample response from the next pages. All diagrams represent causal systems.



