## EECS 120 Midterm 2 Wed. April 9, 2014 1610 - 1730 pm

Name:\_\_\_\_\_\_ SID:\_\_\_\_\_

- Closed book. One 8.5x11 inch page two sides formula sheet (or two single sided). No calculators.
- There are 4 problems worth 100 points total. There may be more time efficient methods to solve problems.

Problem	Points	Score
1	24	
2	28	
3	22	
4	26	
TOTAL	100	

In the real world, unethical actions by engineers can cost money, careers, and lives. The penalty for unethical actions on this exam will be a grade of zero and a letter will be written for your file and to the Office of Student Conduct.

Tables for reference:

$\tan^{-1} 0.1 = 5.7^{\circ}$	$\tan^{-1} 0.2 = 11.3^{\circ}$
$\tan^{-1}\frac{1}{2} = 26.6^{\circ}$	$\tan^{-1} 1 = 45^{\circ}$
$\tan^{-1}\frac{1}{3} = 18.4^{\circ}$	$\tan^{-1}\frac{1}{4} = 14^{\circ}$
$\tan^{-1}\sqrt[6]{3} = 60^{\circ}$	$\tan^{-1}\frac{1}{\sqrt{3}} = 30^{\circ}$
$\sin 30^\circ = \frac{1}{2}$	$\cos 60^\circ = \frac{\sqrt{3}}{2}$
$\cos 45^\circ = \frac{\sqrt{2}}{2}$	$\sin 45^{\circ} = \frac{\sqrt{2}}{2}$

$20\log_{10}1 = 0dB$	$20\log_{10}2 = 6dB$	
$20\log_{10}\sqrt{2} = 3dB$	$20\log_{10}\frac{1}{2} = -6dB$	
$20\log_{10} 5 = 20db - 6dB = 14dB$	$20\log_{10}\sqrt{10} = 10 \text{ dB}$	
$1/e \approx 0.37$	$1/e^2 \approx 0.14$	$\sqrt{2} \approx 1.41$
$1/e^3 \approx 0.05$	$\sqrt{10} \approx 3.16$	$\sqrt{3} \approx 1.73$

### Problem 1. Superheterodyne receiver (24 pts)

Two signals  $x_1(t)$  and  $x_2(t)$  have spectra (Fourier Transforms)  $X_1(j\omega)$  and  $X_2(j\omega)$  respectively, as shown in the figure below. You are given a signal y(t) with spectrum  $Y(j\omega)$ , which contains 2 received signals,  $x_1(t)\cos(\omega_1 t)$  (from station 1) and  $x_2(t)\cos(\omega_2 t)$  (from station 2). A narrow bandpass filter  $H_{IF}(j\omega)$  with fixed center frequency  $\omega_{IF} < \omega_1$  is used to filter out interference.



The block diagram below, when completed, should recover the original  $x_2(t)$  from y(t).

[7 pts] a. Add signal processing elements as necessary in *block1* such that the output  $Z(j\omega)$  will have  $X_2(j\omega)$  in the passband of the bandpass filter. For each element, specify amplitudes and frequencies as necessary.

[10 pts] b. For your block1 system, sketch the spectra  $Z(j\omega)$ , labelling key frequencies and amplitudes.

[7 pts] c. Add signal processing elements as necessary in *block2* such that the output of *block2* is  $x_2(t)$ . For each element, specify amplitudes and frequencies as necessary.



#### Problem 2. Sampling and Discrete Fourier Transform (28 pts)

For parts a) and b), consider the system below, where  $x(t) = \cos(6\pi t)$ . Parts a) and b) may have different  $w(t), T_s, T_o$  and should be answered independently. Sketch should label peak magnitude, and frequency of zero crossing(s) should match given scale.

Note  $\Pi(t) = u(t+0.5) - u(t-0.5).$ 

![](_page_2_Figure_3.jpeg)

![](_page_2_Figure_4.jpeg)

# Problem 2. cont.

 $-24\pi$ 

 $-18\pi$ 

 $-12\pi$ 

 $-6\pi$ 

0

6π

12π

18π

24π

![](_page_3_Figure_1.jpeg)

ω

### Problem 2. cont.

[7 pts] c. Given  $x_3[n] = \cos(\pi n/4)$ , sketch  $X_3[k]$ , the 16 point DFT of  $x_3[n]$ , labelling amplitudes.

![](_page_4_Figure_2.jpeg)

[7 pts] d. Given  $x_4[n] = x_3[n] = \cos(\pi n/4)$  for n even, and  $x_4[n] = 0$  for n odd, sketch  $X_4[k]$ , the 16 point DFT of  $x_4[n]$ , labelling amplitudes.

![](_page_4_Figure_4.jpeg)

## Problem 3. Laplace Transform (22 points)

A causal system with input x(t) and output y(t) is described by the differential equation:

$$\frac{d^2}{dt^2}y(t) + 5\frac{d}{dt}y(t) + 6y(t) = x(t).$$

[11 pts] a. Find Y(s) and y(t) for x(t) = 0 (ZIR).  $y(0^{-}) = 1$ ,  $\frac{d}{dt}y(0^{-}) = 2$ .

$$Y(s) = \underline{\qquad \qquad } \qquad \qquad y(t) = \underline{\qquad \qquad }$$

[11 pts] b. Find Y(s) and y(t) for x(t) = u(t) (ZSR).  $y(0^{-}) = 0$ ,  $\frac{d}{dt}y(0^{-}) = 0$ .

 $Y(s) = \_$ 

$$y(t) =$$
\_\_\_\_\_

Problem 4. Feedback System (26 points)

![](_page_6_Figure_1.jpeg)

[4 pts] a. Find the transfer function for the system above which has input x(t) and output y(t).

$$H(s) = \frac{Y(s)}{X(s)} = \underline{\qquad}$$

[6 pts] b. Find the frequency  $\omega_o$  at which the phase of G(s) is  $-180^{\circ}$ .

 $\omega_o =$ \_\_\_\_\_

[6 pts] c. For the frequency  $\omega_o$  found above, what is the maximum K which could be used before the closed-loop system is unstable (this is the gain margin).

*K* < \_\_\_\_\_

[6 pts] d. Find the sinusoidal steady state response of the closed-loop system with K = 4 to the input  $x(t) = \cos(t)u(t)$ , ignoring any transients. (Hint: phasors).

y(t) =\_\_\_\_\_

[4 pts] e. Without explicitly calculating, discuss the steady-state closed-loop response of the system to  $x(t) = \cos(\omega_o t)u(t)$  using  $\omega_o$  from part b and the K value from part c.