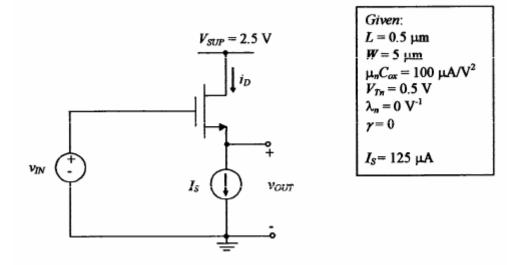
1. MOSFET circuit [17 points]

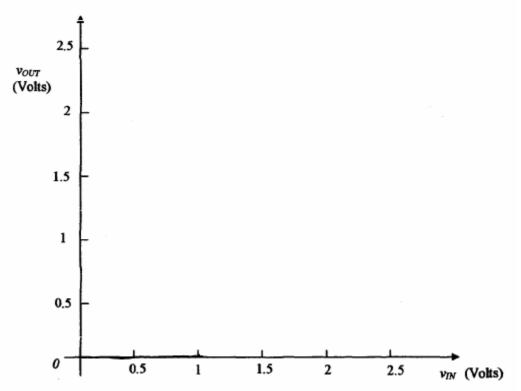


(a) [3 pts.] Assuming that the transistor is operating in saturation, find an equation for the drain current i_D in terms of the input voltage v_{IN} , the output voltage v_{OUT} , and the device parameters. It is *not* necessary to substitute numerical values.

(b) [4 pts.] For v_{IN} = 1.5 V, (i) find the numerical value of the output voltage in Volts and (ii) verify that the transistor is saturated for this case.

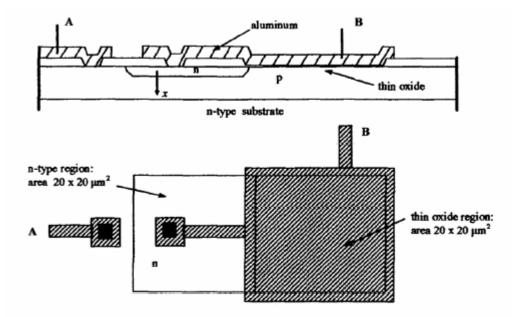
(c) [3 pts.] For $v_{IN} = 0.5$ V, (i) find the numerical value of the output voltage in Volts and (ii) identify the transistor's operating region.

(d) [4 pts.] Sketch the output voltage v_{OUT} as a function of the input voltage v_{IN} over the range $0 \text{ V} \le v_{IN} \le 2.5 \text{ V}$ on the graph below. *Note:* the current source I_S only works for $v_{OUT} > 0 \text{ V}$ and is a short-circuit for $v_{OUT} = 0 \text{ V}$.

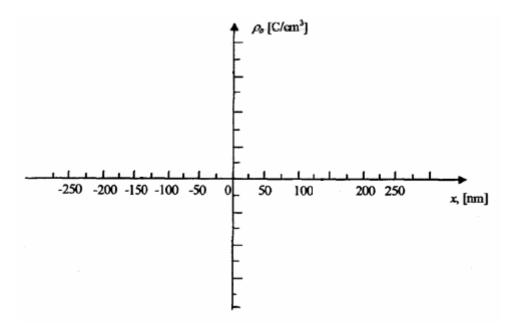


(e) [3 pts.] For a DC input voltage $V_{IN} = 1.5$ V, find the numerical value of the transconductance g_m. If you couldn't solve part (b), you can assume that $V_{OUT} = 0.25$ V for this part (not the correct answer to (b), of course).

2. Integrated charge-storage element [17 points]

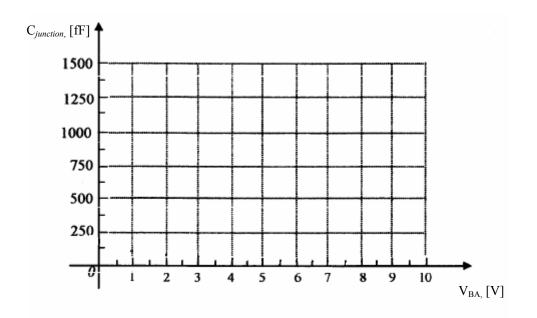


- *Given*: The n region connected to electrode B is doped with phosphorus with $N_d = 2 \times 10^{16} \text{ cm}^{-3}$ and with boron ($N_a = 1 \times 10^{-16} \text{ cm}^{-3}$). The p region connected to electrode A is doped with only boron ($N_a = 1 \times 10^{-16} \text{ cm}^{-3}$). The permittivity of silicon is $\varepsilon_s = 1.035 \times 10^{-12}$ F/cm and the permittivity of oxide is $\varepsilon_{ox} = 3.45 \times 10^{-13}$ F/cm. The thin oxide has a thickness $t_{ox} = 10$ nm. The built-in potential of aluminum is $\varphi_{Al} = -360$ mV
 - (a) [4 pts.] Sketch the charge density in thermal equilibrium along the x axis (see location in the cross section above. *Given*: the width of the depletion region on the p-side of the junction is $x_{po} = 140$ nm = 0.14 µm. Unit charge: $q = 1.6 \times 10^{-19}$ C.

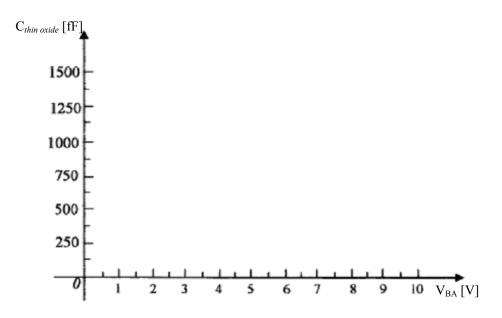


(b) [3 pts.] Find the numerical value of the junction capacitance $C_{junction}(0)$ between the 20 x 20 μ m² n-type region and the underlying p layer in the thermal equilibrium (v_{BA} = 0 V) in fF. *Given*: 1 fF = 10⁻¹⁵ F. *Hint*: the information given in part (a) should be very useful.

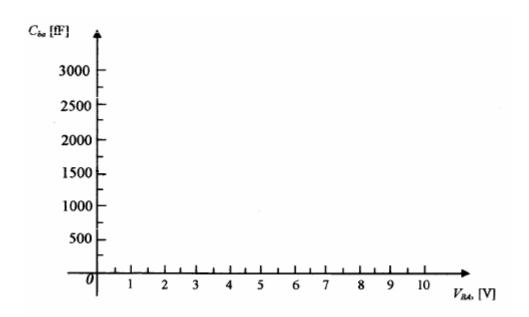
(c) [4 pts.] Plot the junction capacitance versus v_{BA} on the graph below. If you couldn't solve part (b), you can assume that the thermal equilibrium capacitance is 1000 fF in order to do this part.



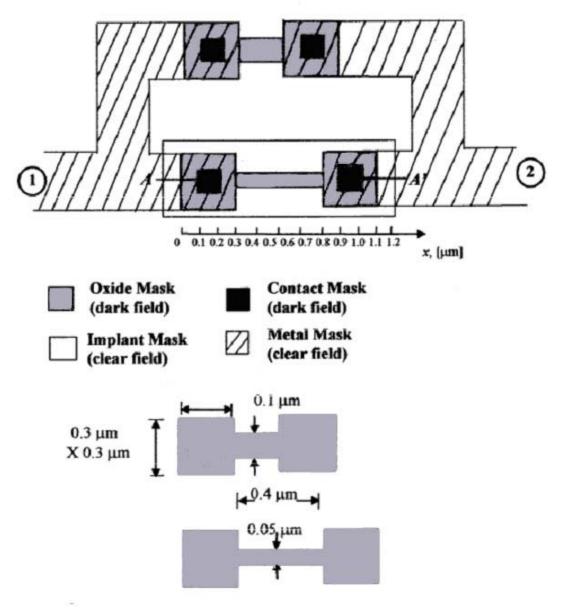
(d) [3 pts.] Sketch the capacitance of the 20 x 20 μ m² thin-oxide area as a function of the voltage V_{AB} on the graph below. *Given*: due to oxide charges, the threshold voltage is V_{Tn} = 4 V, the minimum capacitance of the structure is one-half the maximum capacitance, and the thermal equilibrium capacitance is three-quarters of the maximum.



(e) [3 pts.] Sketch the capacitance C_{ba} as a function of the voltage V_{AB} on the graph below. Ignore the contribution of the overlap of the metal onto the thick-oxide regions.



3. IC resistors [16 points]

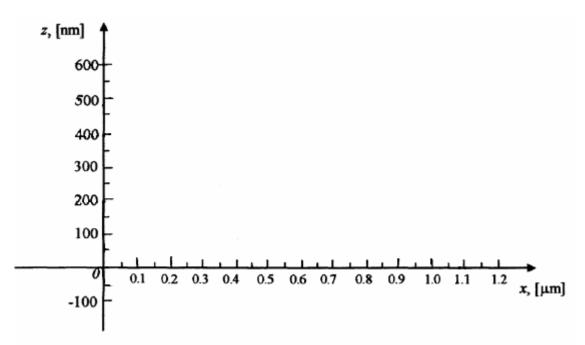


Process Sequence:

- 1. Starting material: boron-doped silicon wafer with a concentration of 2×10^{17} cm⁻³
- 2. Deposit a 0.2 μ m (=200 nm) thick SiO₂ layer
- 3. Pattern the oxide using the **Oxide Mask** (dark field) by etching it down to the silicon. 4. Implant the phosphorus with dose $Q_d = 2 \times 10^{12} \text{ cm}^{-2}$ and anneal to form a 50 nmthick phosphorus-doped regions where the silicon is exposed.
- 5. Spin on photoresist and pattern with the **Implant Mask** (clear field). 6. Implant phosphorus with dose $Q_d = 2 \times 10^{12} \text{ cm}^{-2}$ and then etch off the photoresist.
- 7. Anneal to activate the second implant; the phosphorus regions remain 50 nm thick.
- 8. Deposit a 200 nm-thick SiO₂ layer and pattern using the Contact Mask (dark field).
- 9. Deposit 200 nm of aluminum and pattern using the Metal Mask (clear field).

Given: mobilities for this problem are $\mu_n = 800 \text{ cm}^2/(\text{Vs})$ and $\mu_p = 200 \text{ cm}^2/(\text{Vs})$. The saturation electric field for electrons is $E_{sat} = 1.25 \text{ x} 10^4 \text{ V/cm}$ and their saturation velocity is $v_{sat} = 10^7 \text{ cm/s}$. Count the "dogbone" contact areas as 0.65 square for both resistors.

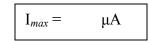
(a) [4 pts.] Sketch the cross section *A*-*A*' on the graph below **after step 9**. *Identify all layers clearly*.



(b) [4 pts.] What is the sheet resistance R_{\Box} of the 0.2 µm long, 0.1 µm wide resistor?

$R_{\Box} =$

(c) [4 pts.] What is the maximum current I_{max} in μ A through the 0.4 μ m long, 0.05 μ m wide resistor?



(d) [4 pts.] Plot the current-voltage curve between terminals 1 and 2 over the range indicated on the graph below

