# **CS61C Summer 2012 Midterm**

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This exam is worth 110 points and will count for 20% of your course grade.

The exam contains 9 questions on 13 numbered pages, including the cover page. Put all answers on these pages; don't hand in stray pieces of paper.

**Question 0:** You will receive 1 point for properly filling out this page as well your login on every page of the exam.

Question	Points (Minutes)	Score
0	1 (0)	
1	15 (26)	
2	10 (14)	
3	10 (18)	
4	9 (16)	
5	10 (18)	
6	17 (26)	
7	12 (22)	
8	26 (40)	
Total	110 (180)	

All the work is my own. I had no prior knowledge of the exam contents nor will I share the contents with others in CS61C who have not taken it yet.

Signature:
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# **Question 1:** Potpourri – Hard to spell, nice to smell... (15 points, 26 minutes)

- a) True/False: (1 pt each)
- T (F) We prefer two's complement over the unsigned representation because two's complement can represent more values. Same number (e.g. 2<sup>32</sup>)
- The assembler uses symbol tables to resolve absolute addresses. Linker's job
- A program will always execute faster in a RISC architecture than a CISC architecture.

  Mix of # instructions, CPI, and clock rate for a particular program can go either way
- T The greater the number of memory accesses in a program, the greater the AMAT.

  AMAT calculated per memory access
- F Pseudo-instructions do not always use \$at.
- $\bigcirc$  F Since \$s0 is a "saved register," it does not need to be saved before any function calls.
- b) Fill in the function below, which returns a new copy of the argument (struct definition not shown):

```
struct something *cpySomething(struct something *old) {
    struct something *new = malloc(sizeof(struct something));
    *new = *old;
    return new; (1 pt each line)
}
```

c) Here is what is currently on the heap:

				_ n	I D	
A	. A			ט	ט ו	

The order of allocation/frees: A allocated, B allocated, C allocated, B freed, D allocated

What allocation strategy was used?

next-fit (2 pts)

d) What is the average CPI of the program described in the table to the right? Which is better: halving memory access cycles or arithmetic cycles and why?

Instruction Category	Cycles	Frequency
Memory Access	10	0.1
Arithmetic	2	0.4
Branch	3	0.2
Comparison	1	0.3

CPI = 10\*0.1 + 2\*0.4 + 3\*0.2 + 1\*0.3 = 2.7 (1pt)

Half mem access: 5\*0.1 + 2\*0.4 + 3\*0.2 + 1\*0.3 = 2.2

Half arithmetic: 10\*0.1 + 1\*0.4 + 3\*0.2 + 1\*0.3 = 2.3, so halving mem access is better

(1 pt w/explanation)

e) I'm getting the message "cannot execute binary file". In one or two sentences, explain what the problem is and how to fix it. (1pt w/explanation)

Assuming not a corrupted file, then the executable was compiled on another machine with a different architecture and can't be read. **Re-compile on the current machine.** 

f) In our 32-bit single-precision floating point representation, we decide to convert one significand bit to an exponent bit. How many **denormalized numbers** do we have relative to before? (Circle one)

More

Fewer Half as many because lost a significand bit (1 pt)

Rounded to the nearest power of 2, how many denorm numbers are there in our new format? (Answer in IEC format) (1 pt)

22 significand bits + sign bit but not counting  $\pm 0$ , so exactly  $2^{23}$ -2 denorms

8 Mebi #s\_\_\_

# **Question 2:** Flippin' Fo' Fun (10 points, 14 minutes)

Assume that the most significant bit (MSB) of x is a 0. We store the result of flipping x's bits into y. Interpreted in the following number representations, how large is the <u>magnitude</u> of y relative to the <u>magnitude</u> of x? Circle ONE choice per row. (2 pts each)

Unsigned	y  <  x	y  =  x	y  >  x	Can't Tell
One's Complement	y  <  x	y	y  >  x	Can't Tell
Two's Complement	y  <  x	y  =  x	y  >  x	Can't Tell
Sign and Magnitude	y  <  x	y  =  x	y  >  x	Can't Tell
Biased Notation (e.g. FP exponent)	y  <  x	y  =  x	y  >  x	Can't Tell

- In unsigned, a number with the MSB of 1 is always greater than one with a MSB of 0.
- In one's complement, flipping all of the bits is the negation procedure, so the magnitude will be the same.
- In two's complement, y is a negative number. Its magnitude can be found by applying the negation procedure, which is flipping the bits and then adding 1, resulting in a larger magnitude than x.
- In sign and magnitude, the  $2^{nd}$  MSB bit will determine the relative magnitudes of x and y, so you can't tell for certain.
- In biased notation, you read the number the same as unsigned but apply a constant bias to BOTH numbers, so the relation is the same as in unsigned numbers.

# Question 3: Doctor Who?!? (10 Points, 18 Minutes)

The Daleks are invading the Earth again, and we need the help of the Doctor! Find the errors in this code and fix them so that the code correctly prints "The 10th Doctor and the Blue Police Box". There is exactly one coding error for each function and function call pair and can be fixed by changing 5 or 6 lines total. Fill in the corrections in the blanks on the opposite page.

```
1
      void whichDoctor(int* input) {
2
          input = 10;
3
      void doctorChanger(char** input1, char** input2) {
5
          char* temp = *input1;
6
          *input1 = *input2;
7
          *input2 = temp;
      }
8
9
      char* policeBoxGiver(char* input) {
10
          *input = "The Master";
11
          return "Police Box";
12
13
      char* colorMaker(void) {
14
          char* color = malloc(sizeof(char) * 4);
          color[0] = 'B';
15
16
          color[1] = '1';
17
          color[3] = 'u';
18
          color[2] = 'e';
19
          color[4] = 0;
20
          return color;
21
      }
22
      char* colorFixer(char* input) {
23
          char temp = *(input+2);
24
          *(input+2) = *(input+1);
25
          *(input+1) = temp;
26
27
      int main(void) {
28
          int * ith = malloc(sizeof(int));
29
          whichDoctor(ith);
30
          char* doctor = "Master";
31
          char* master = "Doctor";
32
          char* details = "and the";
33
          char* color = colorMaker();
34
          colorFixer(color);
35
          char* box = "David Tennant";
36
          doctorChanger(doctor, master);
37
          policeBoxGiver(box);
          printf("The %dth %s %s %s %s",*ith,doctor,details,color,box);
38
39
      }
```

### Line # Corrected Code

```
2 pts
    __2___
          _*input = 10;_____
2 pts
    __14__
          _char* color = malloc(sizeof(char) * 5);_______
1 pt
    24___
          _*(input+2) = *(input+3);_____
    __25__
1 pt
         _*(input+3) = temp;_____
2 pts
   ___36___
         _doctorChanger(&doctor, &master);_____
2 pts
   __37__ _box = policeBoxGiver(box);_____
```

For each answer you did NOT get correct, you -2 pts.

If you <u>added a sixth error</u>, **-1 pt**. (That means if you answered five correct lines and one incorrect line, you received 9 pts).

There were multiple accepted answers for the colorFixer function, which are:

```
23    char temp = *(++input + 2);
(between 22/23)    input++;
34    colorFixer(color + 1);
```

There were also multiple accepted answers for the policeBoxGiver function, which are:

```
11 return strcpy(input, "Police Box");
10 strcpy(input, "Police Box");
```

For line 14, -0.5 pts if you did:

```
char* color = malloc(sizeof(char) * 4 + SOME_VALUE)
```

# **Question 4:** Let Me Float This Idea By You (9 Points, 16 Minutes)

(-1pt if 32 bits used)

For a very simple household appliance like a thermostat, a more minimalistic pricroprocessor is desired to reduce power consumption and hardware costs. We have selected a **16-bit** microprocessor that does not have a floating-point unit, so there is no native support for floating point operations (no float/double). However, we'd still like to represent decimals for our temperature reading so we're going to implement floating point operations in software (in C).

```
(also accepted: unsigned int)

a) Define a new variable type called fp: (1 pt)

_typedef int fp;_______
```

Many people were not sure what to do here. 1 pt was given mainly to those who wrote a valid statement using typedef or the #define directive, or were close. Struct definitions were also accepted.

We have decided to use a representation with a **5-bit exponent field** while following all of the representation conventions from the MIPS 32-bit floating point numbers **except denorms**.

Fill in the following functions. Not all blanks need to be used. <u>You can call these functions and assume proper behavior regardless of your implementation</u>. Assume our hardware implements the C operator ">>" as shift right arithmetic.

#### b) (1 pt)

```
/* returns -num */
fp negateFP(fp num) {
    return _num ^ 0x8000_____;
}
```

If you assumed 32-bit type, then using 0x80000000 was okay.

### c) (1 pt mask/shift, 1 pt bias)

0x7c00 to zero out everything but the exponent field, shift right by 10 to get the unsigned value, then subtract bias of  $2^4 - 1 = 15$  to get the actual signed value.

### d) (1 pt per line)

#### 5 pts total:

<u>First line</u>: 1pt for trying to get the exponent by means of getExp(num) or manually retrieving it.

<u>Second and third line</u>: -0.5 pt each line if the numeric value on the right was close, but not correct.

<u>Fourth and fifth</u>: needed to correctly zero out the exponent field of num, and OR or add the modified exponent back into that field. 1pt for not forgetting to re-add the bias, and 1pt for getting the masking/shifting right.

#### Other:

**−1** pt for left shifting the exponent by n instead of adding.

If you didn't add the 15 bias because in getExp() you didn't subtract the 15 bias, then I didn't mark you off for that.

# **Question 5**: Who Says Less is Better? (10 points, 18 Minutes)

We're going to take a page out of the ARM book and design a new instruction set architecture with just **16 32-bit registers**. This means that we only need 4-bit register fields in our instructions.

a)	How many extra bits do we have now for other fields in	the follow	ving formats?	' (1 pt each)	
	Just the # of register fields per format:	R:	3	J:	_0

b) For R-format instructions, would you give the extra bits to opcode, shamt, or funct? \_\_funct\_\_
 Explain your choice in a sentence or two (no credit without explanation): (2 pts w/explanation)
 Can represent more R-format instructions while maintaining consistent opcode. shamt only needs

to be 5 bits for 32-bit registers. —1 pt if choice was funct but explanation did not include the reason for not picking opcode and shamt.

For I-format instructions, we naturally give the extra bits to the immediate field, resulting in the following format:

```
[ opcode (6) | rs (4) | rt (4) | immediate (18) ]
```

c) What fraction of our address space can we now reach with a branch instruction? (2 pts)

```
_1/4096 = 2<sup>-12</sup>_
```

Address space =  $2^{32}$  B, branch immediate represents  $2^{18}$  instr =  $2^{20}$  B.

People forgot to put it in fraction, but if I saw  $2^{32}$  B for address space and  $2^{18}$  instr =  $2^{20}$  B for branch reach, then I gave 1 pt.

d) Assume our PC currently contains the address 0x08000000. What is the LOWEST address (in hex) we can reach with a branch?

```
___0x07F80004____
```

On a branch,  $new_PC = PC+4 + 4*imm$ . Most negative immediate is  $0\times20000$ , so  $imm*4 = 0\times80000$ . Sign-extended, this becomes  $0\timesFFF80000$ . Then  $0\times08000004 + 0\timesFFF80000 = 0\times07F80004$ .

(1 pt for seeing PC+4, 1 pt for seeing correct lowest branch distance, 1 pt for correct hex math)

e) Write out the Verilog pseudocode (as in the OPERATION column on the MIPS Green Sheet) for beq. Make sure you specify what BranchAddr is. (1 pt)

```
if( R[rs] == R[rt] )
  PC = PC+4 + { 12{immediate[17]}, immediate, 2'b0 }
```

Many, many people did not specify BranchAddr in the form above.

Some people didn't put **12** as the number of times to extend the immediate's sign bit.

## Question 6: Cache in While You Can (17 points, 26 Minutes)

Consider a single 4KiB cache with 512B blocks and a write-back policy. Assume a 32-bit address space.

a) If the cache were direct-mapped, (1 pt each)

```
# of rows? ____8 ___ # of offset bits? ____9 ____
2^{12}/2^9 = 8. \log_2(512) = 9.
```

b) If the cache were 4-way set associative,

```
# of tag bits? _____22___ # of index bits? ____1 # of bits per cache slot? ____4120___
(1 pt) (2 pts)
```

```
8/4 = 2, \log_2(2) = 1. 32 - 1 - 9 = 22. 512*8 + 22 + 2 = 4120. If tag wrong, 512*8 + \text{wrong\_tag} + 2 accepted (if obvious algebraic mistake, -1 pt).
```

Consider an array of the following location structs:

```
typedef struct {
     ... // some undefined number of other struct members
     int visited;
     int danger;
} location;
location locs[NUM LOCS];
```

Here's a piece of code that counts the number of places we've visited. Assume this gets executed somewhere in the middle of our program, that count is held in a register, and the size of the array is greater than 4 KiB.

```
for(int i = 0; i < NUM_LOCS; 1++)
    if(locs[i].visited) count++;</pre>
```

- c) What's the fewest possible number of bytes written to main memory? (1 pt) \_\_\_\_\_0 B\_\_\_\_\_
- d) What's the greatest possible number of bytes written to main memory? (1 pt) \_\_\_\_4 KiB\_\_\_\_

We're reading, not writing. What will be written back are dirty blocks already in the cache.

Now consider if we store the visited and danger information in individual arrays instead:

```
int visited[NUM_LOCS];
int danger[NUM_LOCS];

e) This way, the cache can exploit better ___spatial locality__ for the above task. (1 pt)

We can expect a ____lower___ (higher or lower) miss rate (1 pt)

because of the change in the number of ____compulsory___ (type of cache miss) misses. (1 pt)

(also accepted: read)
```

Consider the following code with NUM\_LOCS > 2^10.

```
for(int i = 0; i < NUM_LOCS; i++)
    if(visited[i] && danger[i] > 5) count++;
```

Two memory accesses are made per iteration: one into visited, the other into danger. Assume that the cache has no valid blocks initially. You are told that in the worst case, the cache has a miss rate of 100%. Consider each of the following possible changes to the cache individually.

f) Mark each as **E**, if it eliminates the chances of this worst-case scenario miss rate, **R** if it reduces the chances, or **N** if it's not helpful. (2 pts each)

•	More sets, same block size, same associativity	R_
•	Double associativity, half block size, same total cache size	E_
•	Everything stays the same but use a write-through policy instead	N_

Given that the worst case miss rate is 100% for blocks that hold more than 1 piece of array data, our cache *must* be direct-mapped. In addition, the worst case happens when the visited and danger arrays start in blocks that map to the same row AND have the same offset.

- With more sets/rows, we are increasing the size of the cache. If the cache size changes such that addresses of visited[i] and danger[i] no longer map to the same row, then we no longer have the worst case scenario. This is not guaranteed to happen, so the chances are reduced.
- Increasing associativity completely removes the ping-pong effect.
- A write-through policy does not change the behavior of the cache at all.

# **Question 7:** Can't Make Copies Fast Enough (12 points, 22 Minutes)

We are revisiting our friend the Fast String Copy from lecture! Recall that the function prototype in C is as follows:

```
char *strcpy(char *dst, char *src);
```

Consider the following MIPS implementation of this function:

```
jal strcpy # begin function call
...
strcpy:
   addi $v0,$a0,0
loop: lb $t0,0($a1)
   sb $t0,0($a0)
   addiu $a0,$a0,1
   addiu $a1,$a1,1
   beq $t0,$zero,exit
   j loop
exit: jr $ra
```

Suppose we are running code on a machine with the following cache parameters:

- Unified L1\$ with a hit time of 2 cycles and a hit rate of 95%
- Miss Penalty to main memory of 200 cycles
- Base CPI of 1.5 (in the absence of cache misses)
- a) Calculate our machine's AMAT: (1 pt)

```
AMAT = HT + MR × MP = 2 + 0.05 \times 200 = 12 cycles (-0.5 pt for algebraic mistake)
```

b) What is the CPI of a single call to stropy with src = "" (the function call includes the jal)?

There are 8 instructions executed, 2 of which are lb/sb. Unified \$ also handles instruction fetches.

```
CPI = CPI_{base} + Accesses/Instr \times MR \times MP = 1.5 + 1.25 \times 0.05 \times 200 = 14  cycles
```

(1 pt data accesses, 1 pt instruction accesses (> 1 accesses/instr), 1 pt CPI calculation)

```
(-0.5 pt for algebraic mistake)
```

c) We decide to add a L2\$ to reduce our AMAT to 6. Our L2\$ has a hit time of 20 cycles. What's the worst Local Hit Rate that will still meet our AMAT goal? (1 pt MR, 1 pt HR)

```
AMAT = HT_1 + MR_1(HT_2 + MR_2 \times MP). Solving with AMAT = 6, we get MR_2 = 0.3, so worst HR_2 of 70%. (-0.5 pt for algebraic mistake, -1 pt for not substituting or substituting incorrect values)
```

d) In addition to speeding up our architecture, we want to speed up our code, so we decide to eliminate the return value (presumably the caller retains a copy of the destination pointer). In this case, the stropy function above can be rewritten in just 6 instructions. Write out this implementation in the blanks below, introducing any necessary labels (don't worry about any label name clashes with stropy).

#### strcpy2:

e) If we call stropy and stropy2 on the same src string of length n+1=N (N *includes* '\0'), what is the ratio of instructions executed in stropy to instructions executed in stropy2 (including the jal)? Leave your answer in terms of N. (3 pts)

```
strcpy executes 6*(N-1)+5+3 instructions (6 instr per full loop, 5 instructions on last loop, plus jal/\$v0/jr) = 6N+2. strcpy2 executes 5*N+2 instructions (5 instr per loop plus jal/jr). So ratio is (6N+2)/(5N+2).
```

1 pt for numerator and denominator (0.5 pt each for counting the instructions in the loop, and 0.5 pt each for counting the rest). 1 pt for strcpy/strcpy2 rather than strcpy2/strcpy.

f) Is the ratio in part (e) the same as the relative performance between these two functions? In a sentence or two, explain why or why not. (1 pt w/explanation)

**No**, performance (latency) is measured in execution time, not instruction count. The ratio in (e) does not take memory accesses into account.

# **Question 8:** Putting the Science in Computer Science (26 points, 40 minutes)

DNA can be called the "alphabet of life." From a *very* simplified view, DNA within a cell produces amino acids, which in turn produce proteins, which are the building blocks for most of your body. Here we'd like to write some code for examining a strand of DNA.

a) DNA is made up of *nucleotides*, which we write shorthand as A, C, G, and T. DNA is in base 4 (quaternary)! Fill in the table below, using the DNA nucleotide symbols in alphabetical order (A < C < G < T). (2 pts each)</li>

0 1 2 3

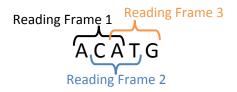
(1 pt given for visible algebraic mistakes)

Decimal	DNA
19	CAT
50	TAG

$$1 \times 4^{2} + 0 \times 4^{1} + 3 \times 4^{0} = 19$$

$$50 = 3 \times 4^{2} + 2 \times 4^{0}$$

An amino acid is encoded by three nucleotides. Because DNA is found in long strands, the following 5 nucleotides can be read 3 different ways:



The sequence **ATG** (as seen in the 3<sup>rd</sup> reading frame) signals the beginning of a protein ("start codon").

b) Fill in the blanks on the opposite page for the **recursive** function find\_start in MIPS that returns the position of the first start codon found in the given strand of DNA. Assume each nucleotide is stored as a char in memory. *Blanks do not necessarily need to be filled*. Maximum points awarded for using the *fewest* amount of registers and memory. **(code on pg. 13, explanation on pg. 14)** 

### [Answer the following AFTER looking at the code]

Assume we call find\_start from main with char dna[] = "GCATGC";.

- c) How many total frames are created on the Stack (not including main)? \_\_\_\_6 (2 pts)\_\_\_\_

  3 frames each for find\_start and strlen. -1 pt for 3.
- d) What is the maximum depth of the Stack (in # of frames, not including main)?

  \_\_\_4 (2 pts)\_\_\_

  3<sup>rd</sup> call of find\_start still calls strlen. -1 pt for 3.
- e) What will the line j ret look like once this file is run through the assembler? \_0x08000000 (1 pt)\_ Object file is in machine language. Absolute address not known, so filled with zeros.
- f) Where will the label ret show up? (Circle one) (2 pts)

Symbol Table Relocation Table Both Neither ret is a label in file, so in symbol table. Also needed later for j ret, so in relocation table. All or nothing for grading.

```
find start:
                                   find start:
                                        addiu $sp,$sp,-4_
     addiu $sp,$sp,-4_ # PROLOGUE
          $ra,0($sp)_ (2 pts)
                                              $ra,0($sp)_
     jal
          strlen # call strlen(dna); jal strlen
             ____ # check end
                                         addi $t0,$v0,-3_
     slti $t0,$v0,3___
                        (4 pts)
                                         slt
                                              $t0,$t0,$a1
     beq
          $t0,$0,chk # check amino acid beq
                                              $t0,$0,chk
     addi $v0,$0,-1 # return -1
                                         addi $v0,$0,-1
     j
          ret
                      # 'ret' for return j
                                              ret
chk: move $t0,$a0____
                        (2 pts) chk: add
                                              $t0,$a0,$a1
     lb
          $t1,0($t0)
                                         lb
                                              $t1,0($t0)
     addi $t2,$0,65
                                         addi $t2,$0,65
     bne
          $t1,$t2,rec
                                         bne
                                              $t1,$t2,rec
     lb
          $t1,1($t0)
                                         lb
                                              $t1,1($t0)
     addi $t2,$0,84___
                          (1 pt)
                                         addi $t2,$0,84___
     bne
          $t1,$t2,rec
                                        bne
                                              $t1,$t2,rec
     lb
          $t1,2($t0)
                                         lb
                                              $t1,2($t0)
     addi $t2,$0,71___
                                         addi $t2,$0,71___
                          (1 pt)
     bne
          $t1,$t2,rec
                                         bne
                                              $t1,$t2,rec
     move $v0,$a1____
                          (1 pt)
                                         move $v0,$a1
     j
          ret
                                         j
                                              ret
rec: addiu $a0,$a0,1
                      (2 pts) rec: addiu $a1,$a1,1__
     addiu $a1,$a1,1___
     jal find start
                                         jal find start
ret:
                                   ret:
          $ra,0($sp)_
                        (2 pts)
                                              $ra,0($sp)_
     lw
                                         lw
     addiu $sp,$sp,_4_
                                         addiu $sp,$sp,_4_
     jr
          $ra
                                         jr
                                              $ra
```

There were multiple ways to correctly fill in the code. Any equivalent lines (MAL and TAL both accepted) were counted provided proper behavior. Two different solutions are shown on the previous page.

In the left column, the recursion is done by incrementing both the pointer and position counter. In this case, the value returned by strlen in v0 decreases with each recursion and you need to check if v0<3 (checking for v0<0 also works). The pointer moves, so you just load characters off of t0=a0.

In the right column, the recursion is done by incrementing just the position counter. In this case, the value returned by strlen in v0 is constant (n) and you need to check if pos>n-3. The pointer doesn't move, so you load characters off of t0=a0+a.

No additional registers were needed beyond what was given (\$t0-\$t2, \$a0, \$a1, \$v0).

—1 pt for each additional register used.

No saved registers are needed and no temporary registers are needed once the recursive call returns, so \$ra is the only register that needed to be saved. -1 pt for each register used that did not follow MIPS register conventions. For example, if you used \$s0, you needed to have saved/loaded it in the prologue/epilogue to avoid losing 2 points instead of 1.

#### **Grading Procedure:**

- 1) Checked prologue and epilogue. -1 pt for not saving \$ra. As noted, -1 pt for each additional register saved (same for around the recursive call).
- 2) Checked choice of recursion implementation. -1 pt for not incrementing \$a1 (function prototype returns an int, not a char \*).
- 3) Checked correct setting of \$t0 at chk label based on recursion choice.
- 4) Checked characters (84 for 'T' and 71 for 'G'). These were on the MIPS Green Sheet or could have been counted from 65 = 'A'. -1 pt if swapped (check for 'AGT' instead of 'ATG').
- 5) Checked return value if start codon found. Needed to be \$a1 (return int, not char \*).
- 6) Bounds checking:
  - -1 pt if jumped to ret without setting \$v0 to -1 (-1 indicates start codon not found, as noted in comments).
  - -2 pts if logic was inverted (returned -1 when should have jumped to chk and vice-versa), chk was unreachable, or used check for other recursion method.
- 7) **–1 pt** for each additional register used and register use that didn't followed register conventions.