# **UC Berkeley - Computer Science**

CS61B: Data Structures

Midterm #2, Spring 2018

This test has 9 questions worth a total of 240 points and is to be completed in 110 minutes. The exam is closed book, except that you are allowed to two double sided written cheat sheets (can use front and back on both sheets). No calculators or other electronic devices are permitted. Give your answers and show your work in the space provided. Write the statement out below in the blank provided and sign. You may do this before the exam begins.

"I have neither given nor received any assistance in the taking of this exam."							

#	Points	#	Points
0	1	6	14
1	24	7	46
2	28	8	46
3	32	9	30
4	0		
5	20		
		TOTAL	240

Name:
SID:
Three-letter Login ID:
Login of Person to Left:
Login of Person to Right:
Exam Room:

Signature:

# Tips:

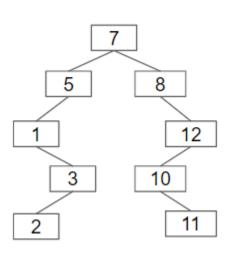
- There may be partial credit for incomplete answers. Write as much of the solution as you can, but bear in mind that we may deduct points if your answers are much more complicated than necessary.
- There are a lot of problems on this exam. Work through the ones with which you are comfortable first. Do not get overly captivated by interesting design issues or complex corner cases you're not sure about.
- Not all information provided in a problem may be useful, and <u>you may not need all lines</u>.
- Unless otherwise stated, all given code on this exam should compile. All code has been compiled and executed before printing, but in the unlikely event that we do happen to catch any bugs in the exam, we'll announce a fix. <u>Unless we specifically give you the option, the correct answer is not 'does not compile.'</u>
- O indicates that only one circle should be filled in.
- $\square$  indicates that more than one box may be filled in.
- For answers which involve filling in a  $\bigcirc$  or  $\square$ , please fill in the shape completely.
- Throughout the exam, assume that hash table resizing takes linear time.

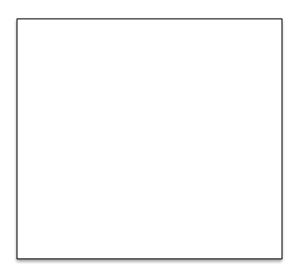
Optional. Mark along the line to show your feelings on the spectrum between $\ \odot$ and $\ \odot$ .	Before exam: [⊜ After exam: [⊝	

**0. So it begins (1 point).** Write your name and ID on the front page. Write the exam room. Write the IDs of your neighbors. Write the given statement and sign. Write your login in the corner of every page. Enjoy your free point  $\odot$ .

### 1. Tree time.

a) (4 points). Suppose we have the BST shown below. Give a valid tree that results from deleting "7" using the procedure from class (a.k.a. Hibbard deletion). Draw your answer to the right of the given tree in the box.





b) (4 points). Give an example of a rotation operation on the original tree from 1a (on the left) that would increase the height. You do not need to draw the tree, just write the operation, e.g. "rotateRight(11)".

c) (4 points). Draw the 2-3 tree that results from inserting 1, 2, 3, 7, 8, 9, 5 in that order.

d) (3 points). Draw the LLRB that results from inserting 1, 2, 3, 7, 8 9, 5 in that order. Write the word "red" next to any red link.

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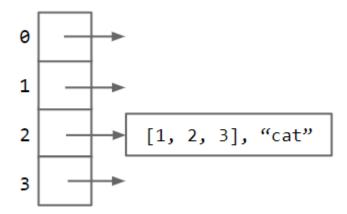
e) (3 points). Draw a valid BST of minimum height containing the keys 1, 2, 3, 7, 8 9, 5.

**f)** (6 points). Under what conditions is a <u>complete</u> BST containing N items <u>unique</u>? By unique we mean the BST is the only complete BST that contains exactly those N items. By complete we mean the same idea that was required for a tree to be considered a heap (not repeated here). Reminder: We never allow duplicates in a BST.

#### 2. Hash Tables.

a) (5 points). Draw the hash table that is created by the following code. Assume that XList is a list of integers, and the hash code of an XList is the sum of the digits in the list. Assume that XLists are considered equal only if they have the same length and the same values in the same order. Assume that FourBucketHashMaps use external chaining and that new items are added to the end of each bucket. Assume FourBucketHashMaps always have four buckets and never resize. The result of the first put is provided for you. Represent lists with square bracket notation as in the example given.

```
FourBucketHashMap<XList, String> fbhm = new FourBucketHashMap<>();
fbhm.put(XList.of(1, 2, 3), "cat");
fbhm.put(XList.of(1, 4), "riding");
fbhm.put(XList.of(5), "a");
fbhm.put(XList.of(3, 4), "bull");
fbhm.put(XList.of(1, 4), "below");
```



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b) (4.5 points). Next to the calls to get, wri	ite the return value of the get call. Assume that get returns
null if the item cannot be found.	
	<pre>fbhm = new FourBucketHashMap&lt;&gt;();</pre>
<pre>XList firstList = XList.of(1, 2,</pre>	3);
<pre>fbhm.put(firstList, "cat");</pre>	
fbhm.get(XList.of(1, 2, 3));	
<pre>firstList.addLast(0); // list is</pre>	now [1, 2, 3, 0]
<pre>fbhm.get(firstList);</pre>	
fbhm.get(XList.of(1, 2, 3));	<del></del>
	te the return value(s) of the get call. Assume that get returns
null if the item cannot be found.	
, ,	<pre>fbhm = new FourBucketHashMap&lt;&gt;();</pre>
<pre>XList firstList = XList.of(1, 2,</pre>	3);
<pre>fbhm.put(firstList, "cat");</pre>	
<pre>firstList.addLast(1); // list is</pre>	now [1, 2, 3, 1]
<pre>fbhm.get(firstList);</pre>	
<pre>fbhm.get(XList.of(1, 2, 3));</pre>	
<pre>fbhm.get(XList.of(1, 2, 3, 1));</pre>	
<pre>fbhm.get(XList.of(3, 4));</pre>	
<pre>fbhm.put(firstList, "dog");</pre>	<del></del>
<pre>fbhm.get(firstList);</pre>	
<pre>fbhm.get(XList.of(1, 2, 3));</pre>	
fbhm.get(XList.of(1, 2, 3, 1));	
d) (4 points). What are the best and worst of	case get and put runtimes for FourBucketHashMap as a
	hMap? Don't assume anything about the distribution of keys.
.get best case: _Θ	
.get worst case: $\_\Theta$	
. put best case: $-\Theta$	
.put worst case $\_\Theta\_$	
e) ( <b>4 points</b> ). If we modify FourBucketHas	shMap so that it triples the number of buckets when the load

e) (4 points). If we modify FourBucketHashMap so that it triples the number of buckets when the load factor exceeds 0.7 instead of always having four buckets, what are the best and worst case runtimes in terms of N? Don't assume anything about the distribution of keys.

.get best case:	
.get worst case:	_Θ
.put best case:	_Θ
.put worst case	_Θ
-	

As noted on the front page, throughout the exam you should assume that a single resize operation on any hash map takes linear time.

## 3. Weighted Quick Union.

a) (10 points). Define a "fully connected" DisjointSets object as one in which connected returns true for any arguments, due to prior calls to union. Suppose we have a fully connected DisjointSets object with <u>6 items</u>. Give the best and worst case height for the two implementations below. The height is the number of links from the root to the deepest leaf, i.e. a tree with 1 element has a height of 0. <u>Give your answer as an exact value</u>. Assume Heighted Quick Union is like Weighted Quick Union, except uses height instead of weight to determine which subtree is the new root.

	Best Case Height	Worst Case Height
Weighted Quick Union		
Heighted Quick Union		

b) (8 points). Suppose we have a Weighted Quick Union object of height H. Give a general formula for the minimum number of objects in a tree of height H as a function of H. Your answer must be exact (e.g. not big theta).

c) (6 points). Draw a Quick Union tree of 6 objects or fewer that would be <u>possible</u> for Heighted Quick Union, but <u>impossible</u> for Weighted Quick Union. If no such tree exists, simply write "none exists."

d) (8 points). Create a set for storing SimpleOomage objects Assume that hashCode for SimpleOomage is the perfect hashcode you were expected to write in HW3, where hash code values are unique and always between 0 and 140,607, inclusive.

**4. PNH (0 points).** This 1996 simulation video game by Maxis had a hidden feature introduced secretly by a programmer, where on certain dates of the year, "muscleboys in swim trunks" would appear by the hundreds and hug and kiss each other.

**5. Multiset.** The Multiset interface is a generalization of the idea of a set, where items can occur multiple times.

For example, if we call add(5), add(5), add(10), add(15), add(5), then the resulting Multiset contains {5, 5, 10, 15, 5}. In this case, multiplicity(5) will return 3.

a) (12 points). A 61B student suggests that one way to implement Multiset is to modify a BST so that it is instead a "Trinary Search Tree", where the left branch is all items less than the current item, the middle branch is all items equal to the current item, and the right branch is all items greater than the current item. The multiplicity is then simply the number of times that an item appears in the tree. Implement the add method below.

```
public class TriSTMultiset<T extends Comparable<T>> implements Multiset<T> {
    private class Node {
        private T item;
        private Node left, middle, right;
        public Node(T i) { item = i; }
    }
    Node root = null;
    public void add(T item) {
        if (p == null) {
            int cmp = item.compareTo(p.item);
            if (cmp < 0) {
            } else if (cmp > 0) {
            }
            return p;
        }
        ...
```

b) (4 points). Let X be an item with multiplicity M, and let N be the number of nodes in the tree. Give an Omega bound for the best case runtime of any possible implementation of multiplicity(X) for a TriSTMultiset. Give the tightest possible bound you can.

$\Omega$ (	,
( )/	
321	

represent the following values:

 $\Box$ A

 $\Box A$ 

 $\square B$ 

 $\square B$ 

 $\Box C$ 

 $\Box$ C

 $\Box D$ 

 $\Box$ D

 $\Box E$ 

 $\Box E$ 

 $\Box$ F

 $\Box$ F

 $\Box G$ 

 $\Box G$ 

 $\Box$ H

 $\Box$ H

 $\square K$ 

 $\square K$ 

 $\Box$ L

 $\Box$ L

 $\square M$ 

 $\square M$ 

Median value:

Largest value:

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### 7. Iteration.

a) (12 points). Fill in the toList method. It takes as input an Iterable<T>, where T is a generic type argument, and returns a List<T>. If any items in the iterable are null, it should throw an IllegalArgumentException. You should use the for each notation. Do not use .next and .hasNext explicitly.

b) (8 points). The ReverseOddDigitIterator implements Iterable<Integer>, and its job is to iterate through the odd digits of an integer in reverse order. For example, the code below will print out 77531.

```
ReverseOddDigitIterator rodi = new ReverseOddDigitIterator(12345770);
for (int i : rodi) {
    System.out.print(i);
}
```

Write a JUnit test that verifies that ReverseOddDigitIterator works correctly using your toList method from before. Use the List.of method, e.g. List.of(3, 4, 5) returns a list containing 3 then 4 then 5.

CS61B MIDTERM, SPRING 2018 Login: \_\_\_\_\_ c) (18 points). Fill in the implementation of the ReverseOddDigitIterator class below. public class ReverseOddDigitIterator implements Iterable<Integer>, Iterator<Integer> { private int value; public ReverseOddDigitIterator(int v) { value = v;public boolean hasNext() { if (value == 0) { return \_\_\_\_\_; // hint: this class should // be implemented } // so that the example return ; // code that prints } else { // **77531** on the previous value = value / 10; // page works. return ; } } public Integer next() { int d = \_\_\_\_\_; value = ; return d; public Iterator<Integer> iterator() { return \_\_\_\_\_; } // assume any classes you need from java.util have been imported d) (8 points). If you didn't complete part c, assume it is completed and compiles. For each of the following, which file (if any) will fail to compile as a direct result of the removal? By "direct result", we mean the compilation failure is not caused by a dependency failing to compile. Suppose we remove "implements Iterable<Integer>", which file will fail to compile? ○ IterableUtils ○ TestRODI ○ ReverseOddDigitIterator ○ None Suppose we instead remove implements Iterator<Integer>, which file will **fail** to compile? ○ TestRODI ○ IterableUtils ○ ReverseOddDigitIterator ○ None Suppose we instead remove the hasNext method, which file will fail to compile? ○ ReverseOddDigitIterator ○ IterableUtils ○ TestRODI ○ None Suppose we instead remove the iterator method, which file will **fail** to compile? ○ IterableUtils ○ TestRODI ○ ReverseOddDigitIterator ○ None

8.	Asym	pto	tics

a) (12 points). Give the runtime of the following functions in  $\Theta$  notation. Your answer should be a function of N that is as simple as possible with no unnecessary leading constants or lower order terms. **Don't spend** too much time on these!

_Θ	publ:	ic sta	tic vo	id g	<b>1(i</b> nt	N) {						
		for	(int i	= 0;	; i < N	l*N*N;	i +=	1) {	{			
		+	•	_	= 0; j			_	1) {			
			Sys	stem.	.out.pr	int("	yhe"	);				
		_	}									
	_	}										
	}											
Θ	publ	ic sta	tic vo	id g	2(int	N) {						
	•				; i < N		= 1) -	{				
		=	int nur	nJ =	Math.p	ow(2,	i + :	1) -	1; //	<	consta	nt time!
		+	for (in	nt j	= 0; j	j < nur	1J; j	+= 1	1) {			
			-	stem.	.out.pr	int("	het"	);				
			}									
	,	}										
	}											
_Θ	pub1	ic sta	atic vo	oid g	g3(int	N) {						
	•	for	(int i	= 2	; i < N	ا; i *=	= i) ·	{}				
		for	(int i	= 2;	; i < N	l; i++)	{}					
	}											
b) (4 points	s). Sup	pose we	have ar	ı algo	rithm wi	th a run	time th	nat is	$\Theta(N^2 lo$	g N) i	n all cas	ses. Which of
				_					,			h information
(NEI)?			•									
O(N <sup>2</sup> log N	1)	O Tı	116	$\bigcirc$	False		NEI					
$\Omega(N^2 \log N)$	-				False		NEI					
$O(N^3)$	•,				False		NEI					
$\Theta(N^2 \log_4 1)$	N)				False		NEI					
- (- · · · · · · · · · · · · ·	•/	<u> </u>		)	- 4100		.,,,,					
c) (6 points	). Supp	ose we	have an	algori	thm with	n a runti	me tha	t is O	$(N^3)$ in a	ıll case	es.	
There exist	ts some	e inputs	for whic	h the	runtime	is $\Theta(N^2)$	)	$\bigcirc$	True	○ F	alse	○ NEI
There exist		-				, ,		Ō	True		alse	○ NEI

○ True

○ True

○ True

○ False

○ False

○ False

There exists some inputs for which the runtime is  $\Theta(N^4)$ 

The worst case runtime has order of growth N<sup>3</sup>

The worst case runtime is  $O(N^3)$ 

O NEI

O NEI

O NEI

d) (12 points). Give the best and worst case runtime of the following functions in $\Theta$ notation. Your answer should be as simple as possible with no unnecessary leading constants or lower order terms. <b>Don't spend</b> too much time on these! Assume $K(N)$ runs in constant time and returns a boolean.
<pre>public static void g4(int N) {     if (N == 0) { return; }     g4(N - 1);     if (k(N)) { g4(N - 1); } }</pre>
Best case: _Θ Worst case: _Θ
<pre>public static void g5(int N) {    if (N == 0) { return; }    g5(N / 2);    if (k(N)) { g5(N / 2); } }</pre>
Best case: _Θ Worst case: _Θ
<pre>e) (6 points). Give the best and worst case runtime of the code below in terms of N, the length of x. Assume HashSets use the idea of external chaining with resizing used in class, and that resize is linear. public Set<planet> uniques(ArrayList<planet> x) {     HashSet<planet> items = new HashSet&lt;&gt;();     for (int i = 0; i &lt; x.size(); i += 1) {         items.add(x.get(i));     }     return items; }</planet></planet></planet></pre>
Best case runtime for uniques: $\_\Theta$ Worst case runtime for uniques: $\_\Theta$
f) (6 points). Consider the same code from part b, but suppose that instead of Planets, x is a list of Strings. Suppose that the list contains N strings, each of which is length N. Give the best and worst case runtime.
Best case runtime for uniques: $\_\Theta$ Worst case runtime for uniques: $\_\Theta$

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9. (30 points). Imagine that we have a list of every commercial airline flight that has ever been taken, stored as an ArrayList<Flight>. Each Flight object stores a flight start time, a flight ending time, and a number of passengers. These values are all stored as ints.

The trick we use to store a flight start time (or end time) as an int, rather than as some sort of Time object, is to store the number of minutes that had elapsed in the Pacific Time Zone since midnight on January 1<sup>st</sup>, 1914, which was the first day of commercial air travel.

For example, a flight taking off at 2:02 PM on March 6<sup>th</sup>, 1917 and landing at 3:03 PM the same day carrying 30 passengers would have takeoff time 1,671,243, landing time 1,671,304, and number of passengers 30.

# Give an algorithm for finding the largest number of people that have ever been in flight at once.

Your algorithm must run in N log N time, where N is the number of total commercial flights ever taken. Your algorithm must not have a runtime that is explicitly dependent on the number of minutes since January 1<sup>st</sup>, 1914, i.e. you can't just consider each minute since that day and count the number of passengers from each minute and return the max.

Your algorithm may use any data structures discussed in the course (e.g. arrays, ArrayDeque, LinkedListDeque, ArrayList, LinkedList, WeightedQuickUnion, TreeMap, HashMap, TreeSet, HashSet, HeapMinPQ, etc.)

a. List any data structures needed by your algorithm, including the type stored in the data structure (if applicable). If you use a data structure that requires a compareTo or compare method, describe <u>briefly</u> how the objects are compared. Do not include the provided ArrayList<Flight> in your list of data structures. Please list concrete implementations, not abstract data types.

b. Briefly describe your algorithm in plain English. Be as concise and clear as possible.