## CS 186/286 Fall 2017 Midterm 1

- Do not turn this page until instructed to start the exam.
- You should receive 1 single-sided answer sheet and a 14-page exam packet.
- You have 80 minutes to complete the midterm.
- The midterm has 5 questions, each with multiple parts.
- You will turn in the answer sheet but not the exam.
- For each question, place only your final answer on the answer sheet; do not show work.
- Use the blank spaces in your exam for scratch paper.
- You are allowed one $8.5 " \times 11^{\prime \prime}$ double-sided page of notes.
- No electronic devices are allowed.


## 1 SQL

Imagine that you are using SQL to program an online card game. You are given a table Deck(suit text, val text, score integer) primary key (suit, val) where each tuple in Deck represents one card to be dealt. The suit is one of 4 possible strings: hearts, spade, club, diamond and the value is one of thirteen possible strings: two, three, four, five, six, seven, eight, nine, ten, jack, queen, king, ace. Assume that Deck represents a standard deck of 52 playing cards.

| suit | val | score |
| :--- | :--- | :--- |
| heart | two | 2 |
| spade | king | 13 |
| $\vdots$ | $\vdots$ | $\vdots$ |

1. (1 point) Which of the following queries is a syntactically valid SQL query that returns $1 / 2$ the score attribute as a floating point number? There is only one correct answer.
A. SELECT FLOAT (score)/2 FROM Deck
B. SELECT score/2 AS FLOAT FROM Deck
C. SELECT CAST (score AS FLOAT)/2 FROM Deck
D. SELECT (FLOAT)score/2 FROM Deck
E. SELECT score:FLOAT/2 FROM Deck
F. None of the above

Solution: C. Recall from the SQL Homework, that Postgres uses the syntax CAST (attr as TYPE). So to return $1 / 2$ the score attribute as a floating point number, the answer is C.
2. (5 points) We want to create a view called Hand that includes all possible distinct draws of two cards from the deck (without replacement) where order does not matter. For example, the view should include either (heart, jack, 11, spade, four, 4) or (spade, four, 4, heart, jack, 11), but not both. Which of the following queries correctly populates the view. There may be zero, one, or more than one correct answer.
A. CREATE VIEW Hand(suit1, val1, score1, suit2, val2, score2) AS

SELECT draw1.*, draw2.*
FROM Deck as draw1, Deck as draw2
WHERE NOT (draw1.suit = draw2.suit AND draw1.val = draw2.val)
B. CREATE VIEW Hand(suit1, val1, score1, suit2, val2, score2) AS

SELECT draw1.*, draw2.*
FROM Deck as draw1, Deck as draw2
WHERE (draw1.suit > draw2.suit OR (draw1.suit = draw2.suit AND draw1.val > draw2.val))
C. CREATE VIEW Hand(suit1, val1, score1, suit2, val2, score2) AS

SELECT draw1.*, draw2.*
FROM Deck as draw1, Deck as draw2
WHERE (draw1.suit < draw2.suit OR (draw1.suit = draw2.suit AND draw1.val < draw2.val))
D. CREATE VIEW Hand(suit1, val1, score1, suit2, val2, score2) AS

SELECT DISTINCT draw1.*, draw2.*
FROM Deck as draw1, Deck as draw2
WHERE NOT (draw1.suit = draw2.suit AND draw1.val = draw2.val)

```
E. CREATE VIEW Hand(suit1, val1, score1, suit2, val2, score2) AS
    SELECT draw1.*, draw2.*
    FROM Deck as draw1, Deck as draw2
    WHERE (draw1.suit < draw2.suit
        AND draw1.val < draw2.val)
```

Solution: B and C. To understand why B and C are the correct solutions, let's first consider a simpler problem with a table with a single attribute. Suppose you had a table $T$ with a single attribute $a$, this query returns all pairs:

```
SELECT t1.a, t2.a
FROM T as t1, T as t2
```

This query will return the set of tuples $(s, t)$ that both includes exact duplicates where $s=t$ and duplicates up to ordering where $(s, t)=(t, s)$. We can remove these by adding the following WHERE statement for any type that supports comparison and ordering:

```
SELECT t1.a, t2.a
FROM T as t1, T as t2
WHERE t1.a > t2.a
```

This WHERE statement clearly removes exact duplicates (since $s$ connot equal to $t$ if $s>t$ ). It also removes duplicates up to orders since both $(s, t)$ and $(t, s)$ cannot be in the result since either $s>t$ or $t>s$. This result is symmetric in the sense that WHERE t1.a < t2.a also achieves the same goal. To extend this idea to tables with multiple attributes, we just need to define a consistent comparison between tuples rather than single attributes. We can use the idea of lexicographic ordering as used in the indexing section of the course. This means that for two tuples $(a 1, a 2)$ and $(b 1, b 2)$, we first compare on the first attribute - if there is a tie we proceed to the subsequent attribute.

$$
\begin{aligned}
& (a 1, a 2)>(b 1, b 2) \equiv(a 1>b 1) \wedge(a 1=b 1 \vee a 2>b 2) \\
& (a 1, a 2)<(b 1, b 2) \equiv(a 1<b 1) \wedge(a 1=b 1 \vee a 2>b 2)
\end{aligned}
$$

Therefore, for the question above there are two acceptable WHERE statements:

```
WHERE (draw1.suit > draw2.suit
    OR (draw1.suit = draw2.suit AND draw1.val > draw2.val))
WHERE (draw1.suit < draw2.suit
    OR (draw1.suit = draw2.suit AND draw1.val < draw2.val))
```

So the solution is B and C.
3. (4 points) The total score of a two-card hand is simply the sum of the scores of the two cards. We want to write a query over the Hand view that assigns the total score to each tuple in Hand. Which of the following SQL queries results in the correct output. There may be zero, one, or more than one correct answer.
A. SELECT t.suit1, t.val1, t.suit2, t.val2, SUM(score) AS score

FROM (
SELECT suit1, val1, suit2, val2, score1 AS score FROM Hand
UNION
SELECT suit1, val1, suit2, val2, score2 AS score FROM Hand

```
    ) as t
    GROUP BY t.suit1, t.val1, t.suit2, t.val2
B. SELECT suit1, val1, suit2, val2, SUM(COALESCE(score1, score2)) AS score
    FROM Hand
    GROUP BY suit1, val1, suit2, val2
C. SELECT h1.suit1, h1.val1, h2.suit2, h2.val2, h1.score1 + h2.score2 AS score
    FROM Hand AS h1, Hand AS h2
    WHERE h1.suit1 = h2.suit2 AND h1.val1 = h2.val2
D. SELECT suit1, val1, suit2, val2, score1 + score2 AS score
    FROM Hand
    GROUP BY suit1, val1, suit2, val2, score1, score2
```

Solution: D. For this question, it actually would suffice the run the following query:

SELECT suit1, val1, suit2, val2, score1 + score2 AS score
FROM Hand

This query is much simpler than those provided in the choices so the trick is to determine which of provided queries is equivalent to this query under the assumptions laid out in the previous two sections.

- Choice A is incorrect if there exists a record where score1 is equal to score2, this means that the UNION statement will turn that into a single tuple and not aggregate properly.
- Choice B is incorrect because COALESCE takes the returns the first non-null value, this is not the same as adding the two scores.
- Choice C is conceptually incorrect as it would create a new table where both val1 and val2 are equal to each other.
- Choice D is correct because under the problem assumptions all hands are uniquely identified by the suits and values of their cards. This means that the GROUP BY statement returns a single tuple and there is no table aggregate in the SELECT statment-making it equivalent to not using it at all.


## 2 Heap Files

Assume that we have serialized a relation as an 8 MB heap file on disk without any header pages of any sort. Further assume that file is divided into 64 KB pages ( $1 \mathrm{MB}=1000 \mathrm{~KB}$ ). Answer the following questions with the following important notes in mind.

- Reuse results: For each part of this question, whenever possible you should reuse the values calculated in previous parts using capital letters, e.g. let $A$ be your answer in part $\mathrm{A}, B$ be your answer in part $B$, etc. Do not use the numerical value of previous parts in subsequent parts.
- Spare the arithmetic: You can leave arithmetic expressions unsimplified.
A. (1 point) How many pages are in the file? Remember the notes above!

Solution: The file takes up $8 \mathrm{MB}(8000 \mathrm{~KB})$ and one page holds 64 KB , so the file takes up $8000 / 64=125$ pages.
B. (1 point) Imagine we want to add a page directory to the heap file. If 24 directory entries can fit on one page, how many additional directory pages do we need for the file? Remember the notes above!

Solution: This question is poorly worded and caused a lot of confusion during the exam. For that reason, we were very lenient on the answer.
The original intent of the question was to ask for the total number of directory pages. Since 24 entries fit on one page and we need one entry for each of $A$ data pages, the total number of directory pages is $\left\lceil\frac{A}{24}\right\rceil$.
However, the clarification given during the midterm specified that it should be the number of directory pages beyond 1 . For that reason we accepted both $\left\lceil\frac{A}{24}\right\rceil$ and $\left\lceil\frac{A}{24}-1\right\rceil$ as correct answers.
C. (1 point) Assume that at least one page in the file has space for a new record. In the worst case, how many I/Os does it take to insert a new record into the relation and persist the changes to the file? Remember the notes above!

Solution: Conceptually, we want to find a page with free space, update the page, and update its directory page. To find the page with free space we have have to scan the directory pages, $B \mathrm{I} / \mathrm{Os}$. To update the page we read it in then write it back out, $2 \mathrm{I} / \mathrm{Os}$. To update the directory page, since it's already read into memory, we just need $1 \mathrm{I} / \mathrm{O}$ to write it back out. This is a total of $B+3 \mathrm{I} / \mathrm{Os}$. If we consider $B$ to be the "beyond- 1 " number of directory pages, the solution is $B+4 \mathrm{I} / \mathrm{Os}$.
D. (2 points) In the worst case, if you are given the value of the primary key of an existing record, how many I/Os does it take to update that record? Remember the notes above!

Solution: It was clarified during the exam that records were fixed length (so the size of an updated record is the same size as the original record). To update a record in a heap file, you must scan the entire file to find it, then update it and write it back out. The page directory is not involved in the search for the record. This will take $A+1$ I/Os.
E. (2 points) Now imagine we sort the file by the relation's primary key. Given the value of the primary key of an existing record, how many I/Os will it take to update that record in the worst case? Remember the notes above!

Solution: It would only take $\log _{2}(A)$ I/Os to find the record in a sorted file. However, in the worst case, we update the column that the file is sorted on and have to end up shifting records on all $A$ pages. Therefore, this will take $\log _{2}(A)+2 A$ I/Os in the worst case.

## 3 B+-Trees

1. (1 point) What is the maximum fanout $F$ of an order $d \mathrm{~B}+$-tree?

Solution: The maximum fan out is the maximum occupancy plus one, or $2 d+1$, by definition. Some students interpreted the question as asking how many entries can be in the leaf node, so we also accepted $2 d$ to account for this. (Moreover, we also accepted $F+1$ based on how $F$ is interpreted in the previous problem)
2. (2 points) Assume that each leaf can hold $F$ data entries. What is the maximum number of data entries that an order $d \mathrm{~B}+$-tree of height 5 can store? Note that a height $1 \mathrm{~B}+$-tree only has a root node, and a height $2 \mathrm{~B}+$-tree has a root node and one layer of leaf nodes. Express your answer as a function of $F$

Solution: We are assuming that the leaf pages hold $F=2 d+1$ entries instead of the standard $2 d$. At height 1 , the root node is a leaf node and therefore the index holds $F$. At height 2 , there is a root node and its children are leaf nodes. The root node has a max fanout of $F$ children and each child is a leaf node that can hold max $F$ entries. Therefore the index can hold $F^{2}$ total entries. Generally, the tree holds $F^{h}$ entries by similar justification and at height 5 , the tree can hold up to $F^{5}$ entries. We are accepting $F^{5},(2 d+1)^{5}$ and any other fifth power of fanout
3. (2 points) Again, assume that each leaf can hold $F$ data entries. What is the minimum number of I/Os it will take to check if a data entry exists in a B+-tree with $1,000,000,000\left(1 \times 10^{9}\right)$ records assuming we have indexed the file with an order $d$ B+-tree? Express your answer as a function of $F$

Solution: To check if a tree exists in a B+-tree with the minimum number of I/Os we assume that the maximum number of entries are being stored in the inner and leaf nodes. Therefore there will be $\frac{10^{9}}{F}$ leaf nodes. At every level we reduce the number of node we will look at by $\frac{F-1}{F}$ due to the binary search like properties of $\mathrm{B}+$ trees. Therefore it will take us $1+\log _{F}\left(\frac{10^{9}}{F}\right) \mathrm{I} / \mathrm{Os}$ to check if a key exists in the tree.

Consider the following $\mathrm{B}+$ tree of order 2 .

4. (1 point) How many nodes split when you insert 27 ?

## Solution:

- To insert 27 , we follow the rightmost pointer in the tree from the root node because $27>$ $8,27>13,27>20,25>20$.
- We get to the leaf node containing $(25,28,31,32)$ and attempt to insert 27 , but the leaf node is at maximum capacity and the insertion breaks the occupancy invariant. Therefore we must split the leaf into $(25,27)$ and $(28,32,21)$ and copy up key 27 because this is a leaf node.
- We attempt to insert 27 into the parent node containing $(8,13,20,25)$ but the root is also at maximum capacity. We split it into $(8,13)$ and $(25,28)$ pushing up key 20 because it is an inner node. Our final tree looks like and we split two nodes

5. (1 point) After inserting 27 into the tree, you also insert 26 . How many nodes split as a result of inserting $26 ?$

## Solution:

- To insert 26 , we first look at the root node and follow the right pointer because $26 \geq 20$. We then follow the middle pointer at the inner node below the root node because $26>25$ but $26<28$. We get to the leaf node containing $(25,27)$
- We attempt to insert 26 into the leaf node containing $(25,27)$ and since 3 is less than the occupancy invariant 4 we insert 26 and are done. We did not split any nodes.

6. (1 point) Assume that after inserting 26 and 27 , you insert the keys $34,35,36, \ldots, 100$. After all these insertions, what keys are in the leftmost leaf node?

Solution: You should be able to identify that we are only inserting keys into the right side of the tree. This is similar to bulk loading in that the left leaf nodes will not be touched. Therefore, we know that the leftmost leaf node will not be modified and will contain $(2,7)$ after the insertions to the right side of the tree.
7. (1 point) In homework 2, which class was used to represented keys in a $B+$ tree? There is only one correct answer.
A. Atom
B. DataBox
C. DbType
D. Datum
E. Scalar
F. AtomicVal
G. Value
H. None of the above.

Solution: The answer is DataBox. None of the other classes exist at all in the homework.

## 4 External Sorting

Assume pages are 2 KB large. Also assume you have a 12 KB buffer pool with six 2 KB frames.

1. (2 points) How many passes $P$ would it take to externally sort an 84 page file? Include the initial sorting pass and subsequent merging passes in your answer. You do not need to simplify your answer.

Solution: In general, we can sort $N$ pages with $B$ buffer pages in $1+\left\lceil\log _{B-1}\left(\left\lceil\frac{N}{B}\right\rceil\right)\right\rceil$ passes. Here, $N=84$ and $B=6$, so it takes $1+\left\lceil\log _{5}\left(\left\lceil\frac{84}{6}\right\rceil\right)\right\rceil=3$ passes.
2. (2 points) What would be the total cost in $\mathrm{I} / \mathrm{Os}$ for this external sort? Let $P$ be the answer to part 1 (i.e. the number of passes). Leave your answer in terms of $P$. You do not need to simplify your answer.

Solution: In all $P$ passes, we read and write all 84 pages of the file. Thus, the total cost is $2 * 84 * P=168 P=504 \mathrm{IOs}$.
3. (2 points) What is the minimum number of additional buffer frames we require to reduce the number of passes $P$ (from part 1) by 1? You do not need to simplify your answer.

Solution: With 6 buffer frames, we can sort the file in three passes. In order to sort the file in two passes, we need $B$ buffer frames where $B(B-1) \geq 84$. The smallest such $B$ is 10 . Thus, the number of additional pages is $10-6=4$.

True or False
4. (1 point) Increasing the number of buffer pages does not affect the number of $I / O s$ performed in Pass 0 of an external sort.

Solution: True. Regardless of the number of buffer pages, every pass of an external sort (including Pass 0 ) performs the same number of IOs.
5. (1 point) Double buffering reduces the time it takes to sort records within a single page.

Solution: False. Double buffering allows a program to concurrently perform computations and fetch data from disk. Once a page of data is resident in memory, double buffering will not help speed up computation on it.

## 5 Buffer Management

We are given an initially empty buffer pool with 4 buffer frames. Consider the following access pattern:

```
SEEMAWESOMEPOSSUM
```

In the next two questions, you will need to evaluate the MRU replacement policy, keeping track of the pages in the buffer pool, and the number of buffer pool hits.

1. (2 points) Using an MRU replacement policy, what are the four pages in the buffer pool after all accesses are complete? Note: write the four pages in alphabetical order.

Solution: MPUW. See Figure 1.
2. (1 point) Using an MRU replacement policy, how many buffer pool hits are there?

Solution: 8. See Figure 1.

| S |  |  |  |  |  |  | $*$ | O |  |  |  | $*$ | S | $*$ | U |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | E | $*$ |  |  |  | $*$ |  |  |  | $*$ | P |  |  |  |  |  |
|  |  |  | M |  |  |  |  |  | $*$ |  |  |  |  |  |  | $*$ |
|  |  |  |  | A | W |  |  |  |  |  |  |  |  |  |  |  |

Figure 1: MRU

We are again given an initially empty buffer pool with 4 frames. Now consider the following access pattern:

## S E EMAWESOME

Note: This access pattern is different from the previous question. Do NOT include POSSUM in your accesses.

In the next few questions, you will need to evaluate the clock policy, keeping track of the pages in the buffer pool, the reference bits on the frames, and the number of buffer pool hits. Assume that we do not increment the clock hand when we request a page that is already in the buffer pool. Only increment the clock hand as part of a page replacement.
3. (2 points) Using the clock replacement policy, what are the four pages in the buffer pool after all accesses are complete? Note: write the four pages in alphabetical order.

## Solution: EMOS. See Figure 2.

4. (1 point) Using the clock replacement policy, what are the reference bits for each buffer pool page? Note: make sure your reference bits correspond to the pages in alphabetical order. For example, put 1110 if the first 3 pages have a reference bit set, but the last page does not.

Solution: 1100. Before the last 2 accesses ( $M$ and $E$ ), the pages in the buffer pool are in the following order W, E, S, O. The reference bits are set as 1011 , and the clock arm is pointing at W. Now, when we request $M$, the clock arm sets the reference bit for $W$ to be 0 , and moves onto $E$. The reference bit for $E$ is not set, so it replaces $E$ with $M$ and sets the reference bit for $M$ to be 1 (so the buffer pool pages are now in the order W, M, S, O, and the reference bits are 0111). The clock arm is now pointing at S . Now, when we request E , the clock arm advances until it reaches a reference bit of 0 , so it moves through S and O and sets their reference bits to 0 . Then, the clock arm points at W and replaces it with E . The final state is thus $\mathrm{E}, \mathrm{M}, \mathrm{S}$, O, where E and M have their reference bits set to 1 .
5. (1 point) Using the clock replacement policy, how many buffer pool hits are there?

Solution: 2. See Figure 2.

| S |  |  |  |  | W |  |  |  |  | E |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | E | $*$ |  |  |  | $*$ |  |  | M |  |
|  |  |  | M |  |  |  | S |  |  |  |
|  |  |  |  | A |  |  |  | 0 |  |  |

Figure 2: Clock

True or False.
6. (1 point) Assume page A is loaded into the buffer pool during a specific access pattern and is not evicted at any point during the access pattern. Page A has a pin count of 7 at the end of all accesses. True or False: Page A was accessed exactly 7 times during this access pattern.

Solution: False. At any point of an access pattern, the pin count of a page represents the number of processes currently accessing the page, not the total number of times the page was accessed. Here is a counterexample: Page A could've been requested 8 times. The pin count went up to 8 , but then a process was done using page A and decremented its pin count to 7.
7. (1 point) The buffer manager decides when to set the dirty bit of a page.

Solution: False. The file/index management code decides when to set the dirty bit of a page.
8. (1 point) A buffer pool has 101 frames, and you have an access pattern of 1000 accesses with the following properties:

- 900 of the 1000 page accesses are to the same page $P$.
- The remaining 100 accesses are all to pages that are unique/different from each other and are not to P.

You repeat this access pattern many times. True or False: MRU would have fewer misses than LRU for this access pattern.

Solution: False. Your buffer pool size is 101 frames. You only have 101 unique pages in your 1000 page access pattern. Thus, all the 101 pages in your access pattern can fit inside your buffer pool, so you never have to evict any pages. This means any buffer replacement policy will have the same number of misses ( 0 misses), since you never have to replace pages.

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