You have fifty minutes to complete this test. Please put your login on each sheet, as indicated, in case pages get separated. Answer all questions in the space provided on the exam paper. Show all work (but be sure to indicate your answers clearly.) The exam is worth a total of 20+ points (out of the total of 200), distributed as indicated on the individual questions.

You may use any notes or books you please—anything unresponsive. We suggest that you read all questions before trying to answer any of them and work first on those about which you feel most confident.

You should have 4 problems on 4 pages.

1. _______________ / 6

2. _______________ / 6

3. _______________

4. _______________ / 8

TOT _______________ / 20
1. [6 points] Consider a really simplified set of regular expressions (call them RSREs) consisting of letters ‘a’ and ‘b’, concatenation, union (using the symbol ‘|’), epsilon (represented by the letter e), and Kleene star, but without parentheses. So, for example,

\[ a \ | \ ab \ | \ a^*b \ | \ b \ | \ ba \]

are valid RSREs.

a. Write a regular expression that recognizes RSREs. Use just the basic operators supplied by Flex or JFlex.

b. Draw a DFA that recognizes RSREs.
2. [6 points] Now consider a pretty simple set of regular expressions (we’ll call them PSREs) that are just like RSREs from the first problem except that they also allow parentheses for grouping. As usual, when not grouped by parentheses, Kleene star has highest precedence, followed by concatenation, and finally by union.

a. Write an unambiguous grammar for PSREs. Be sure to observe precedence properly, or you’ll have trouble with part b.

b. Write actions for the grammar of part (a) so that the semantic value you assign to the start symbol is length of the shortest string recognized by the regular expression being parsed. For example, for the PSRE ‘ab’, the actions of your grammar should compute the value 2; for ‘a | bb’ compute 1; for ‘e’ and for ‘(ab)* | c’ compute 0.
3.  [1 point] I noticed that a certain kind of prepackaged snack sold in our local coffee shops has the slogan “The ones you remember,” which I thought was mildly clever. Why?

4.  [8 points] Consider the parse tree below. All terminal symbols are written at the same level on the bottom row.

   ![Parse Tree Image]

   a. Show as much of the grammar as one can deduce from this parse tree.

More questions on the next page
b. Show a reverse rightmost derivation corresponding to this tree, as performed by a shift-reduce parser. (However, you need not mention the shifts and reductions, just the sentential forms that get you back to the start symbol from the input).

c. Show that the grammar is ambiguous by giving a string that has (at least) two parses and giving two distinct parse trees for it.

Continued on next page.
d. Given one of the parse trees for an ambiguous string in this language, can you find two leftmost derivations that give rise to that parse tree? If so, show such a tree and show the derivations; otherwise say why you cannot.