# Final <br> EE40 <br> Fall 2011 

NAME: $\qquad$ SSID: $\qquad$

## Instructions

Read all of the instructions and all of the questions before beginning the exam.
There are 5 problems in this exam. The total score is 130 points. Points are given next to each problem to help you allocate time. Do not spend all your time on one problem.

Unless otherwise noted on a particular problem, you must show your work in the space provided, on the back of the exam pages or in the extra pages provided at the back of the exam.

Draw a BOX or a CIRCLE around your answers to each problem.
Be sure to provide units where necessary.

GOOD LUCK!

| PROBLEM | POINTS | MAX |
| :---: | :---: | :---: |
| 1 |  | 25 |
| 2 |  | 25 |
| 3 |  | 20 |
| 4 |  | 35 |
| 5 |  | 25 |

"Failure is always an option"

- Disgruntled CS Guy
(I assume he repeated this so many times to get on the final)
Problem 1 Warm up (25 points)
Consider the following circuit:


In the box below, provide your answer in this form or LOSE POINTS (if there are extra equations, just write them in as well):

| v1 |  | $v 2$ |  | $v 3$ | + | $v 4$ | = |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| v1 | $+$ | $v 2$ | $+$ | $v 3$ | + | $v 4$ | = |
| $v 1$ | + | $v 2$ | + | $v 3$ | + | $v 4$ | $=$ |
| v1 | $+$ | $v 2$ | $+$ | $v 3$ | $+$ | $v 4$ | = |
| $v 1$ | + | $v 2$ | + | $v 3$ | + | $v 4$ | = |

## Solution:

Problem 2 RC circuits (25 points)

a) Consider the circuit above. If $\mathrm{Vs}(\mathrm{t})=\mathrm{V}_{\mathrm{DD}}{ }^{*} \mathrm{u}(\mathrm{t}) \mathrm{V}$ provide an expression for $\mathrm{V}_{\text {out }}(\mathrm{t})$. You can assume $\mathrm{V}_{\text {OUTI }}(0)=\mathrm{V}_{\text {DD }} .(5$ points $)$
$\mathrm{V}_{\text {outi }}(\mathrm{t})=$
b) Now consider the case where we connect the following two modules together:


Notice the first module is the same as that in a) and the second is very similar.
Notice the two switches close on different conditions!
If:

- $\mathrm{Vs}(\mathrm{t})=\mathrm{V}_{\mathrm{DD}} * \mathrm{u}(\mathrm{t})$
- $\quad \mathrm{V}_{\text {OUT1 }}(0)=\mathrm{V}_{\mathrm{DD}}$
- $\mathrm{V}_{\text {OUt2 }}(0)=0$

Provide a $\underline{\text { SYMBOLIC }}$ expression for how long it takes for $\mathrm{V}_{\text {OUT2 }}>\mathrm{V}_{\mathrm{DD}} / 2$. ( 10 points)

## $\mathrm{t}_{\text {vout2 }}(\mathbf{s})=$

c) Repeat b) exactly but with the following slightly modified circuit.


If:

- $\mathrm{Vs}(\mathrm{t})=\mathrm{V}_{\mathrm{DD}} * \mathrm{u}(\mathrm{t})$
- $\quad \mathrm{V}_{\text {OUT1 }}(0)=\mathrm{V}_{\mathrm{DD}}$
- $\operatorname{V}_{\text {out2 }}(0)=0$

Provide a $\underline{\text { SYMBOLIC }}$ expression for how long it takes for $\mathrm{V}_{\text {OUT2 }}>\mathrm{V}_{\mathrm{DD}} / 2$. ( 10 points)
$\mathbf{t}_{\text {vout2 }}(\mathbf{s})=$
"I don't see much sense in that," said Rabbit.
"No," said Pooh humbly, "there isn't. But there was going to be when I began it. It's just that something happened to it along the way."
-Winnie the Pooh

## Problem 3 DC Op Amps (20 points)

Consider the circuit below.

a) Provide a SYMBOLIC expression for $\frac{v_{x}}{v_{i n}}$
(10 points)
b) Provide a SYMBOLIC expression for $\frac{v_{\text {out }}}{v_{\text {in }}}$ (10 points)
-Pablo Picasso

## Problem 4 Transfer functions

Consider the circuit below:

a) Provide a SYMBOLIC EXPRESSION for the transfer function $H(\omega)=\mathrm{V}_{0} / \mathrm{V}_{\mathrm{S}}$ (10 points)
(So I thought of making the exam purely symbolic, but then the memegenerator post made me realize I couldn't do this... so here are some numbers) ©
b) Assuming the following component variables, list the frequencies (in rad/s) of each zero in the transfer function. (5 points)
$\mathrm{R} 1=1 \mathrm{k} \Omega, \mathrm{R} 2=20 \Omega, \mathrm{C} 1=5 \mu \mathrm{~F}$, and $\mathrm{C} 2=25 \mathrm{nF}$

## Solution:

c) Assuming the following component variables, list the frequencies (in rad/s) of each pole in the transfer function. (5 points)
$\mathrm{R} 1=1 \mathrm{k} \Omega, \mathrm{R} 2=20 \Omega, \mathrm{C} 1=5 \mu \mathrm{~F}$, and $\mathrm{C} 2=25 \mathrm{nF}$

## Solution:

d) Assuming the following component variables, draw the magnitude and phase Bode plots in the semilog paper below. (10 points)
$\mathrm{R} 1=1 \mathrm{k} \Omega, \mathrm{R} 2=20 \Omega, \mathrm{C} 1=5 \mu \mathrm{~F}$, and $\mathrm{C} 2=25 \mathrm{nF}$
DO NOT FORGET TO LABEL THE X AND Y AXES OR YOU WILL LOSE POINTS!


e) In THREE WORDS OR LESS, what does this circuit do? (5 points)
—Douglas Adams, Hitchhiker's Guide to the Galaxy,

## Problem 5 Second order systems (25 points)

Consider the circuit below.


Design a passive circuit inside the black box which will produce an oscillating signal at 13.56 MHz once the switch is opened. The amplitude of the oscillation need not be constant but the frequency should not change with time.

- The available inductor ranges are $0.1 \mu \mathrm{H}-1 \mathrm{mH}$
- The available capacitor ranges are $10 \mathrm{pF}-10 \mu \mathrm{~F}$
- The available resistor ranges are $100 \Omega-100 \mathrm{M} \Omega$.
- There must be at least one resistor in the design.
a) Draw your circuit in the box below and label all components. Make sure to draw wired between all the input and output terminals. (7.5 points)

b) Given the component ranges, what is the highest Q achievable? (7.5 points)
c) What is the bandwidth for this Q? (5.0 points)
d) Change the value of one or more resistors in your design such that the circuit no longer oscillates. At what resistor value(s) is the boundary between oscillation and no oscillation? (5 points)

