

University of California College of Engineering Department of Electrical Engineering and Computer Sciences

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EECS 16B: FALL 2015—MIDTERM 2

Important notes: Please read every question carefully and completely – the setup may or may not be the same as what you have seen before. Also, be sure to show your work since that is the only way we can potentially give you partial credit.

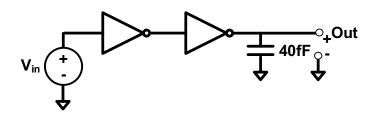
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- Total: ____/ 66

PROBLEM 1. Miscellaneous (18 points)

a) (6 pts) Assuming that for every inverter in the chain shown below, $R_{on,n} = R_{on,p} = 1k\Omega$, and $C_{g,n} = C_{g,p} = 20$ fF, what is the delay from V_{in} transitioning from 0V to V_{dd} to V_{out} transitioning from V_{dd} to 0V?



b) (6 pts) Sketch the phase (in radians) vs. $log(\omega)$ for the filter specified below with $\omega_1 = 1e3$ rad/s and $\omega_2 = 1e6$ rad/s.

$$H(\omega) = \frac{j\omega/\omega_1}{(1+j\omega/\omega_1)} \frac{10}{(1+j\omega/\omega_2)}$$

Hint: You may want to figure out the phase responses of each component of $H(\omega)$ individually and then combine them together.

c) (6 pts) It turns out that filters can be realized not only be electrical components like we have seen so far in class, but out of mechanical (and even electromechanical) components as well. The differential equation provided below represents the relationship between an applied force F(t) (that could be coming from for example an incoming audio signal) and the displacement x(t) of a mass connected to a spring and damper; *m* is the mass, *b* is the damping coefficient, and *k* is the spring constant. If we define $H(\omega) = x(t) / F(t)$ for a sinusoidal F(t), derive $H(\omega)$ for this mechanical filter.

$$m\frac{d^2x(t)}{dt^2} + b\frac{dx(t)}{dt} + kx(t) - F(t) = 0$$

PROBLEM 2. Underwater Communications (28 pts)

Communicating underwater can be very challenging for a number of reasons, and one of the techniques adopted by submarines is to use *subsonic* signals – that is, very low frequencies – for communication. In this problem we'll explore the design of such a communication system for an underwater autonomous robot called FiShT33n.

Important Note: This problem has many sub-parts, but it has been set up in a way that you can complete each sub-part without having gotten the (correct) answer to the previous parts.

a) (2 pts) For our initial design, let's assume that FiShT33n communicates by sending signals that can have frequency components anywhere between -15Hz and 15Hz (i.e., the bandwidth is 30Hz, centered at 0Hz), and that the measured frequency of the signal is used to convey the desired command or message. Given these specifications, what is the minimum frequency that FiShT33n should use to sample the received signal?

(As additional clarification and an example of how the communication works, if the robot's human monitor sends a signal $x(t) = cos(2\pi*10Hz*t)$ and FiShT33n sees that it is receiving a signal whose frequency corresponds to 10Hz, that would mean "stop and search this area". Similarly, if the monitor sends a signal $x(t) = cos(2\pi*5Hz*t)$ and FiShT33n receives a signal whose frequency corresponds to 5Hz, that would mean "get away – a shark is about to try and eat you".) b) (4 pts) Let's assume that your answer to part (a) was 40Hz, that you chose to have FiShT33n's receiver sample at this frequency in order to save power, and that you tried to save some money by not put any filtering in front of the receiver. After some initial failed experiments with FiShT33n out in the ocean, you realize that the robot is sometimes getting confused by the presence of audio signals from things like dolphins, whales, humans, and boats, and that these signals are all at frequencies of 400Hz and above.

Assuming that all interfering signals are at a frequency of exactly 410Hz, after sampling, what continuous-time frequency would FiShT33n's receiver perceive the interfering signal as being equivalent to?

c) (6 pts) Continuing to assume that FiShT33n samples the received signal at 40Hz and that external interference is always at frequencies of 400Hz and above, select a value for ω_c so that the $H(\omega)$ provided below attenuates the interfering signals by at least a factor of 50 while attenuating the desired signal by at most 10%. (In other words, $||H(\omega)|| < 1/50$ for frequencies associated with the interference, while for frequencies associated with the signal $||H(\omega)|| > 0.9$.)

$$H(\omega) = \frac{1}{\left(1 + j\omega / \omega_c\right)^2}$$

d) (8 pts) Assuming that your answer to part (c) was $\omega_c = 2\pi * 100$ Hz, design an analog circuit that realizes this $H(\omega)$. You can use any combination of op-amps and passive components to implement this circuit, but be sure to label the values of any of these passive components.

e) (8 pts) One of your colleagues who didn't take EE16 and has an irrational aversion to analog circuits suggests that instead of adding the filter in, maybe you could just increase the sampling rate of the receiver to 1.52kHz instead. You believe there is a way to make this work, but you worry that this will substantially increase the power dissipated by the microcontroller that implements the receiver.

Let's assume that with the original sample rate of 40Hz, you could operate the microcontroller at a supply voltage $V_{dd} = 0.6V$, and that the microcontroller dissipates 100µW at this frequency (40Hz)/supply voltage (0.6V). If the resistance of the gates inside of the microcontroller is proportional to $1/(V_{dd} - 0.55V)$, what V_{dd} would you need to use to run the microcontroller at 1.52kHz (to support the increased sampling frequency)? How much power will the microcontroller dissipate at this V_{dd} /clock frequency (1.52kHz)?

PROBLEM 3. Controlling a Car (22 points)

In this problem we will examine a simple model for a car driving on a road. The state of the car is $x[k] = [z[k] v[k]]^T$, where z[k] is the position of the car at time kT_s , v[k] is the velocity of the car at time kT_s , and T_s is the sampling period. The car is driven by a force u[k] from its engine, which must counter a friction force $F_f[k]$. Finally, y[k] represents the variables that we will measure (sense). In this case, we can model the dynamics of the car as follows:

$$x[k+1] = Ax[k] + B(u[k] - F_f[k])$$
$$y[k] = Cx[k]$$

$$A = \begin{bmatrix} \lambda_1 & 0.1 \\ 0 & \lambda_2 \end{bmatrix}, B = \begin{bmatrix} 0.01 \\ 0.2 \end{bmatrix}$$

Note: for parts (a) through (c) of this problem, you can assume that the friction force $F_f[k] = 0$ for all k.

a) (4 pts) Let's assume that $C = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ and that we want to set the velocity and

position to some desired values $z_d[k]$ and $v_d[k]$ by using closed-loop control with a forward gain matrix $K = [k_1 \ k_2]$. Provide expressions for the A_{CL} and B_{CL} matrices you would use to create a state-space model of the resulting closed-loop system.

b) (4 pts) Assuming that $\lambda_{CL1} = 1$ and $\lambda_{CL2} = 2$, derive the eigenvalues of A_{CL} as a function of k_1 and k_2 . Note: You do not need to actually solve for the eigenvalues – please just show the equation you would need to solve to find the eigenvalues. c) (6 pts) Assuming that the eigenvalues of A_{CL} are $\lambda_1 = (1-0.1*k_1)$ and $\lambda_2 = (2-0.4k_2+0.1*k_1^2)$ (note that this may or may not be the correct answer to part (b)), explain whether you would choose to use a controller with $K = [k_1 \ k_2] = [5 \ 1]$ or $K = [1 \ 5]$. You should be as clear and complete as possible in identifying the issues/tradeoffs when justifying your selection.

d) (8 pts) Now let's use a potentially more realistic model where the friction force $F_f[k]$ actually depends on the velocity as follows: $F_f[k] = \mu^* v[k]$. Assuming the same feedback system as part (a), derive new expressions for the A_{CL} and B_{CL} matrices including this velocity dependent friction.

e) (BONUS: 6 pts) Recall that the discrete-time state-space model we provided you for the car is actually the result of sampling the continuous-time inputs (in this case, position z(t) and velocity v(t)) going in to our sensors. Let's assume that the road the car is driving on is rough in a way that the continuous time velocity is actually $v(t) = v_{nom}*[1+0.5*\cos(2\pi*100\text{Hz}*t)]$ and that our sensor is sampling with $T_s = 100\text{ms}$. If the sensor directly samples v(t), as a function of v_{nom} , what will the sensor's output v[k] be? Assuming that we set $v_d[k]$ to a fixed constant value, what would this result (i.e., the relationship between v_{nom} and v[k]) imply about the actual average velocity of the car?