

FINAL EXAMINATION

NAME: _____
Last First

Signature

STUDENT ID#: _____ E-MAIL: _____

INSTRUCTIONS:

1. Use the values of physical constant provided below.
2. **SHOW YOUR WORK.** (Make your methods clear to the grader!)
3. Clearly mark (underline or box) numeric answers. Specify the units on answers whenever appropriate.

Physical Constants

Description	Symbol	Value
electronic charge	q	1.6×10^{-19} C
electron rest mass	m_0	9.1×10^{-31} kg
thermal voltage at 300K	kT/q	0.026 V
Boltzmann constant	k	8.62×10^{-5} eV/K

$(kT/q) \ln(10) = 0.060$ V at $T = 300$ K

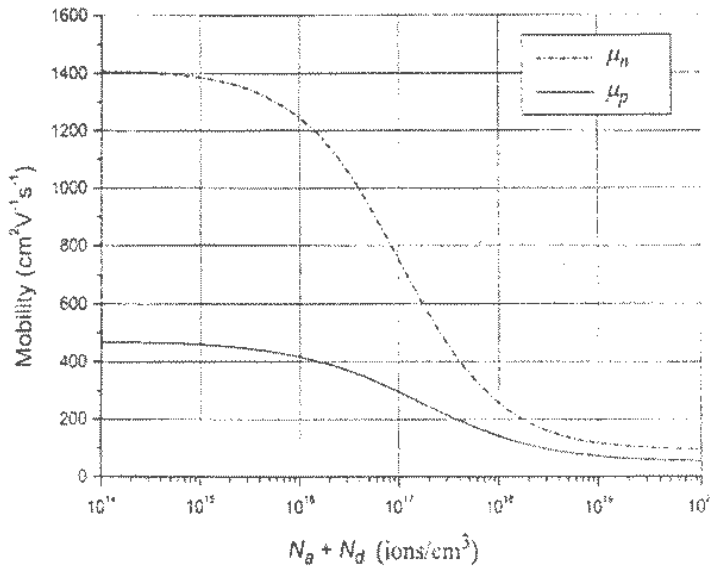
Properties of SiO₂ at 300K

Description	Symbol	Value
band gap	E_g	9 eV
permittivity	ϵ_{SiO_2}	3.45×10^{-13} F/cm
electron affinity	χ_{SiO_2}	0.95 V

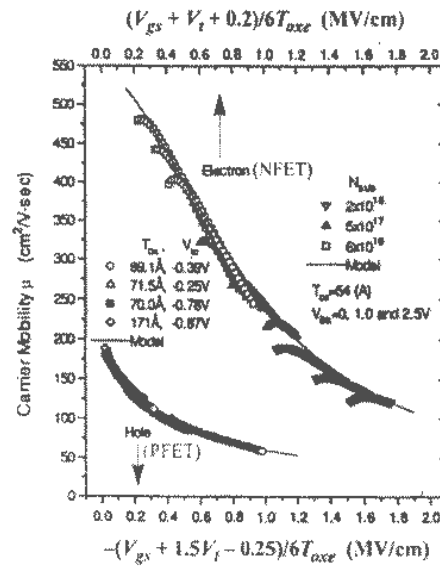
Properties of Silicon at 300K

Description	Symbol	Value
band gap	E_g	1.12 eV
intrinsic carrier density	n_i	10^{10} cm ⁻³
permittivity	ϵ_{Si}	1.0×10^{-12} F/cm
electron affinity	χ_{Si}	4.03 V

Electron and Hole Mobilities in Silicon at 300K



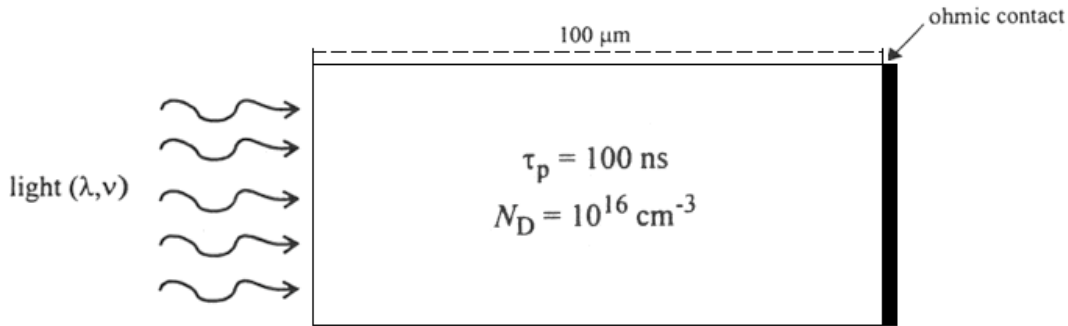
Field-Effect Mobilities in Si at 300K



- 1 _____ / 30
- 2 _____ / 30
- 3 _____ / 40
- 4 _____ / 30
- 5 _____ / 30
- 6 _____ / 40
- Total: _____ / 200

Problem 1: Semiconductor Fundamentals [30 points]

Consider the following uniformly doped n-type Si sample of length $100\ \mu\text{m}$, maintained at $T = 300\text{K}$:



Light incident on the surface is absorbed at $x = 0$, resulting in $\Delta p_{n0} = 10^8/\text{cm}^3$ excess holes at $x = 0$. (The generation rate for $x > 0$ is zero.)

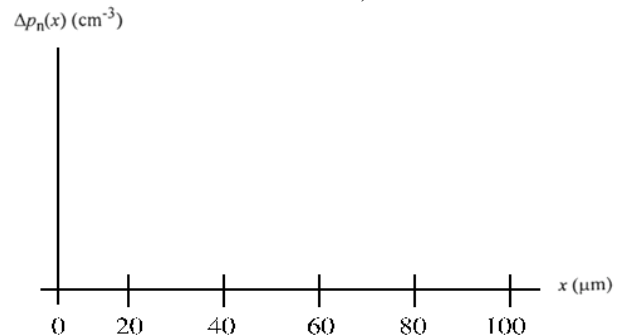
a) Describe the carrier actions (drift, diffusion, recombination-generation) in this sample. [5 pts]

b) i) Write a differential equation (simplest form possible) for the excess hole concentration Δp_n , for $x > 0$. [5 pts]

ii) What is the general solution for this differential equation? [2 pts]

iii) What boundary conditions must $\Delta p_n(x)$ satisfy? [2 pts]

iv) Solve for $\Delta p_n(x)$ and sketch it accurately on the axes provided below. Indicate the maximum value, and the point at which $\Delta p_n(x)$ falls to $1/e$ of the maximum value. [3 pts]



c) Draw the high-band diagram for this sample, indicating the positions of the quasi-Fermi levels for electrons and holes (F_N and F_p , respectively) relative to the intrinsic Fermi Level E_i . [5 pts]

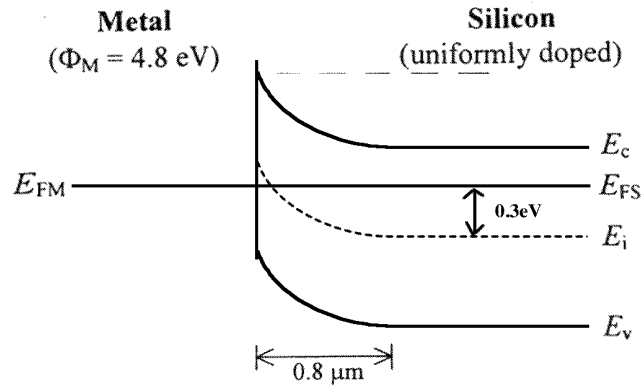
d) Do low-level injection conditions prevail throughout this sample? Justify your answer. [2 pts]

e) Do equilibrium conditions prevail throughout this sample? Justify your answer. [2 pts]

f) Estimate the resistivity of this sample. [4 pts]

Problem 2: Metal-Semiconductor Contact [30 points]

The following is the equilibrium ($T = 300\text{K}$) energy-band diagram for an ideal metal-semiconductor contact:



a) Label the Schottky barrier height (ϕ_B) and built-in voltage (V_{bi}) on the band diagram above. Calculate the values of ϕ_B and V_{bi} . [6 pts]

b) Is this a rectifying or ohmic contact? Explain why. [3 pts]

c) What does qV_{bi} represent? (Why is there a built-in voltage?) [2 pts]

d) Sketch the energy-band diagram for this M-S contact with 0.3 V forward bias applied ($V_A = 0.3 \text{ V}$). Indicate qV_A on your diagram. [5 pts]

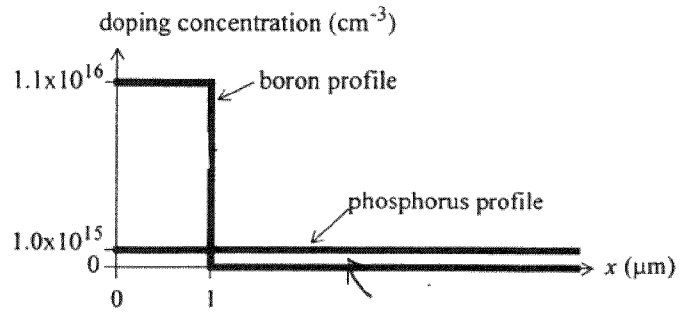
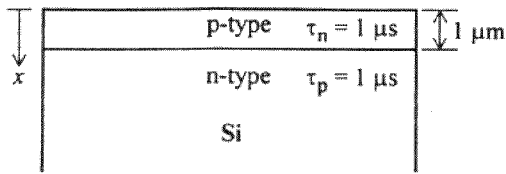
e) Explain how the doping concentration in the silicon can be determined from capacitance measurements. **[8 pts]**

f) Sketch the equilibrium energy-band diagram for a metal ($\phi_M = 4.8$ eV) contact of degenerately doped n-type silicon. Why is this practically an ohmic contact? **[6 pts]**

Problem 3: pn Junction Diode [40 points]

A pn diode is formed by introducing boron into the surface region of a Si sample uniformly doped with phosphorus:

schematic cross-section of diode



a) Draw the equilibrium ($T = 300\text{K}$) energy-band diagram for this diode. Indicate the position of E_F relative to E_i in the quasi-neutral regions. (Numerical values are required.) Label the depletion width W and built-in potential V_{bi} , and calculate their values. [15 pts]

b) Sketch the energy-band diagram for this diode with a large reverse bias applied. Use this diagram to explain how reverse-bias breakdown occurs. [5 pts]

c) Suppose a forward bias of 0.6 V is applied to this diode: (Note that $[\exp(qV_A/kT)] = 10^{10}$)

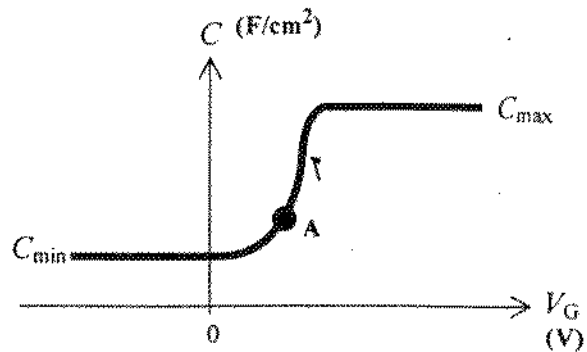
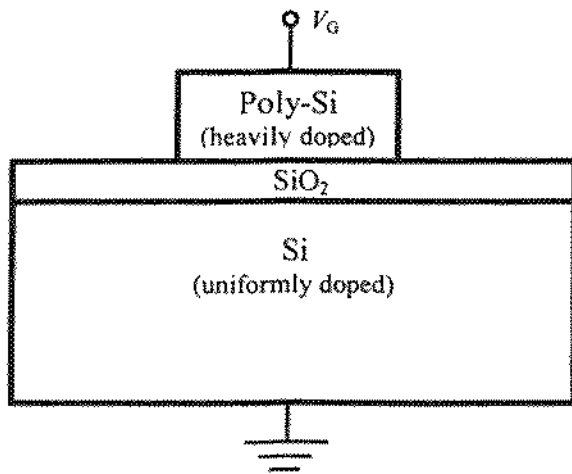
i) Sketch the excess minority carrier profiles in the quasi-neutral regions. Indicate their values at the edges of the depletion region. **[6 pts]**

ii) Estimate the total amount of excess minority carrier charge (in units of C/cm^2) stored in the diode. **[4 pts]**

iii) Estimate the diode current density. **[5 pts]**

iv) Suppose the diode is suddenly shut off at $t = 0$ by disconnecting it from the circuit, so that no current flows for times $t > 0$. Show how the excess minority carrier charge on the n-side changes, for $t > 0$. Estimate the time required for the diode voltage to reach 0 V. **[5 pts]**

Problem 5: Metal-Oxide-Semiconductor Capacitor [30 pts]



a) Was this C - V characteristic measured using a high-frequency ac signal, or low-frequency ac signal? How do you know? [3 pts]

b) Is the Si substrate n-type, or p-type? Justify your answer. [3 pts]

c) Is the poly-Si gate doped heavily in n-type or p-type? Justify your answer. [3 pts]

d) Sketch the MOS energy-band diagram corresponding to the gate bias at point A on the C - V curve. [6 pts]

e) Describe how you would obtain the following parameters from the C - V data:

i) gate-oxide thickness (T_{ox}) [3 pts]

ii) substrate doping concentration (N_{sub}) [4 pts]

iii) flatband voltage (V_{FB}) [4 pts]

iv) fixed oxide charge density (Q_F) [3 pts]

Problem 6: MOS Field-Effect Transistor [40 points]

a) In a certain CMOS technology, the electrical oxide thickness is $T_{\text{oxe}} = 3.45 \text{ nm}$, the body-effect factor is $m = 1.2$, and the absolute value of the threshold voltage of a long-channel MOSFET is $|V_T| = 0.4 \text{ V}$.

i) Sketch the I_D vs. V_{DS} characteristic for an n-channel MOSFET of channel width $W = 1 \text{ }\mu\text{m}$, channel length $L = 1 \text{ }\mu\text{m}$, and gate bias $V_{GS} = 1.5 \text{ V}$. Indicate the values of $V_{D\text{sat}}$ and $I_{D\text{sat}}$. [10 pts]

ii) For what channel lengths will the effect of velocity saturation be significant (*i.e.* resulting in a reduction in $I_{D\text{sat}}$ by more than a factor of 2)? $v_{\text{sat}} = 8 \times 10^6 \text{ cm/s}$. [5 pts]

b) Short-Answer Questions

i) What does the factor m in the MOSFET drain current (I_{DS}) equation account for? (Why is it needed in order to accurately predict the drain current flowing in a MOSFET?) **[4 pts]**

ii) for a given process technology (*i.e.* fixed gate-oxide thickness, source/drain junction depth, and channel doping concentration), why does the magnitude of V_T decrease at very short channel lengths L ? **[4 pts]**

iii) How does the leakage current of a MOSFET change with increasing temperature? Justify your answer. **[4 pts]**

c) Indicate in the table below (by checking the appropriate box for each line) the effect of **decreasing the gate oxide thickness (T_{oxe})** on the performance parameters of an n-channel MOSFET. Provide brief justification for each of your answers. [12 pts]

MOSFET parameter	increases	decreases	remains the same	
Transconductance (g_m)				
Body effect parameter (γ)				
Subthreshold swing (S)				