

**University of California at Berkeley**  
**College of Engineering**  
**Dept. of Electrical Engineering and Computer Sciences**

**EE 105 Midterm I**

Spring 2002

Prof. Roger T. Howe

March 6, 2002

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Your Name: \_\_\_\_\_

Student ID Number: \_\_\_\_\_

***Guidelines***

Closed book and notes; one 8.5" x 11" page (both sides) of *your own notes* is allowed.

You may use a calculator.

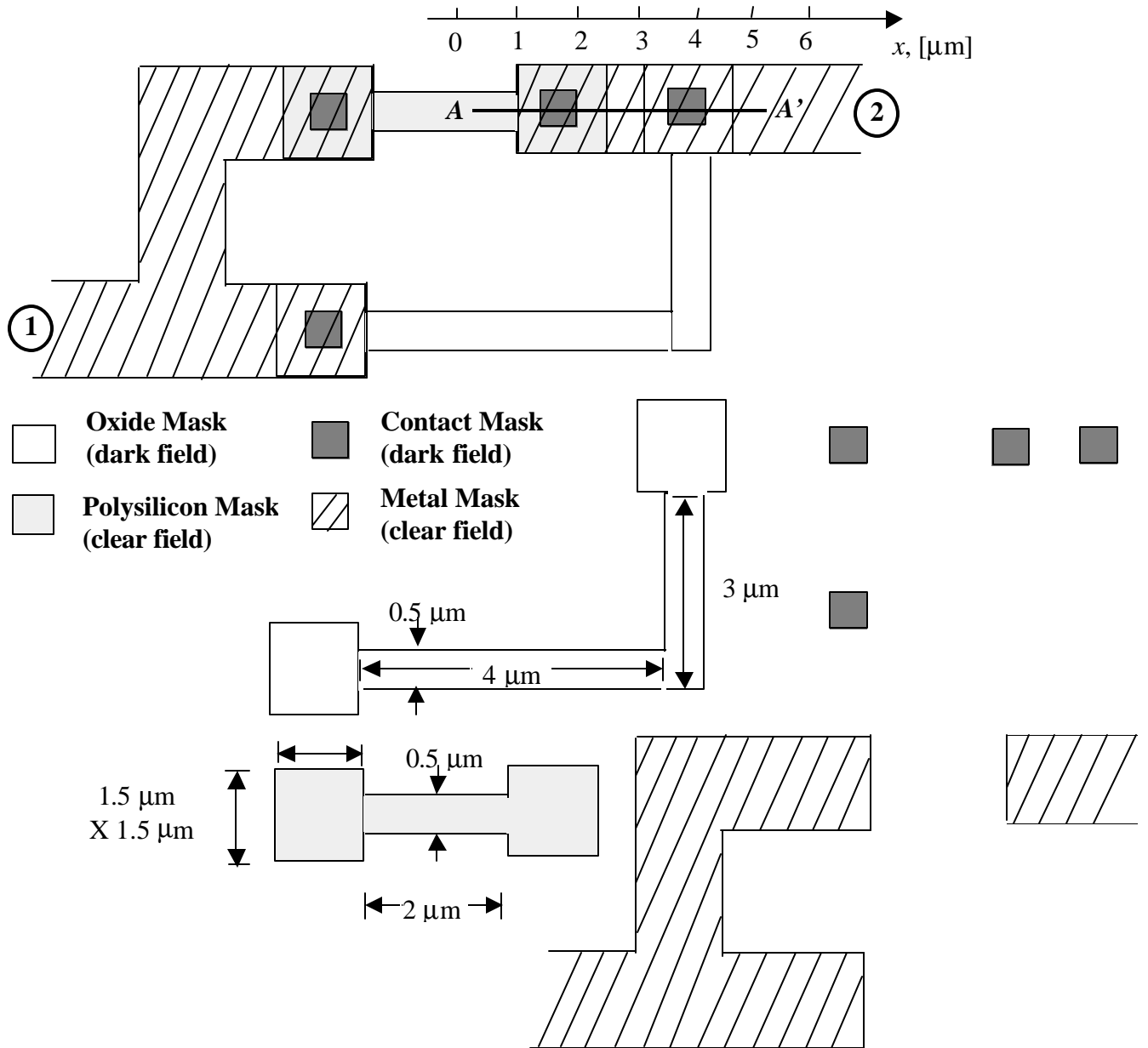
Do not unstaple the exam.

Show all your work and reasoning on the exam in order to receive full or partial credit.

***Score***

Problem	<i>Points Possible</i>	Score
1	17	
2	17	
3	16	
<b><i>Total</i></b>	50	

1. IC resistors [17 points]

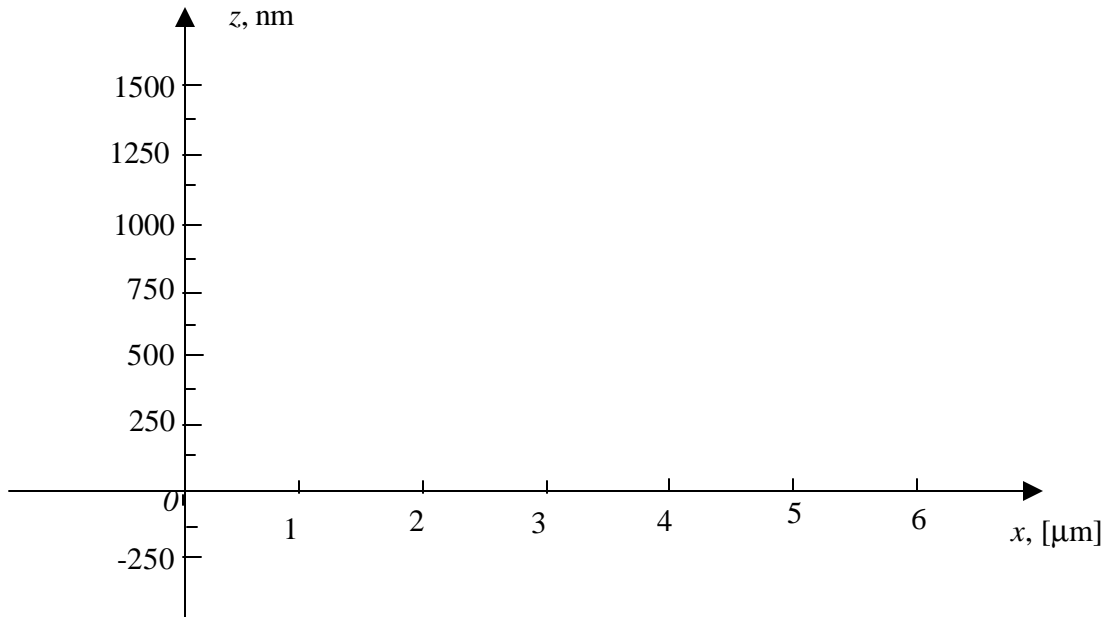


**Process Sequence:**

1. *Starting material:* p-type silicon wafer with a doping concentration of  $1 \times 10^{17} \text{ cm}^{-3}$
2. Deposit a 250 nm-thick  $\text{SiO}_2$  layer
3. Deposit a 250 nm-thick layer of n-type polysilicon and pattern using the **Polysilicon Mask** (clear field).
4. Pattern the oxide using the **Oxide Mask** (dark field).
5. Implant phosphorus with dose  $Q_d = 5 \times 10^{12} \text{ cm}^{-2}$  and anneal to form a 250 nm-thick phosphorus-doped region.
6. Deposit a 250 nm-thick  $\text{SiO}_2$  layer and pattern using the **Contact Mask** (dark field).
7. Deposit 250 nm of aluminum and pattern using the **Metal Mask** (clear field).

**Given:** mobilities for this problem are  $\mu_n = 500 \text{ cm}^2/(\text{Vs})$  and  $\mu_p = 200 \text{ cm}^2/(\text{Vs})$  for both silicon and polysilicon). The saturation electric field for electrons in polysilicon or silicon is  $E_{sat} = 2 \times 10^4 \text{ V/cm}$  and their saturation velocity is  $v_{sat} = 10^7 \text{ cm/s}$ . The mobile electron concentration in the polysilicon is  $n = 10^{17} \text{ cm}^{-3}$  at the end of the process. Count the “dogbone” contact areas as 0.65 square each and the corner square as 0.56 squares in finding the resistance.

(a) [5 pts.] Sketch the cross section **A-A'** on the graph below **after step 7**. Identify all layers clearly.



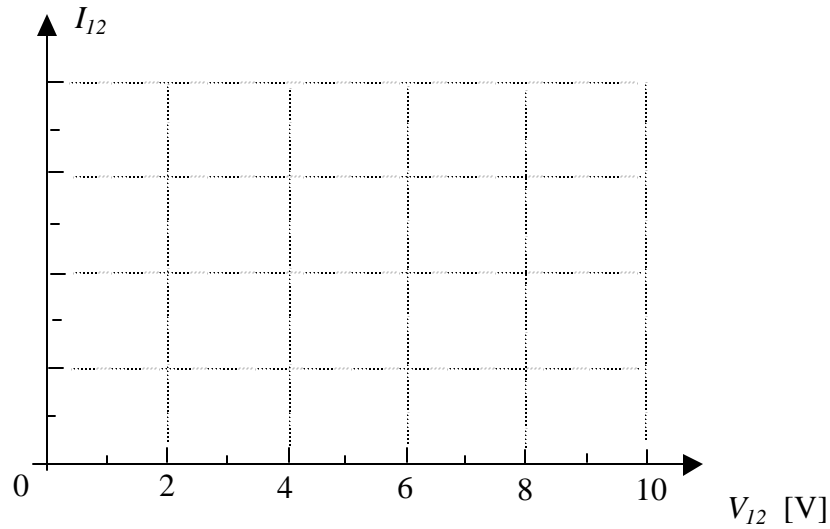
(b) [3 pts.] What is the sheet resistance  $R$  of the  $0.25 \mu\text{m}$ -thick silicon region formed in step 5?

$R =$

(c) [3 pts.] What is the maximum current  $I_{max}$  in  $\mu\text{A}$  through the polysilicon resistor?

$I_{max} =$	$\mu\text{A}$
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(d) [3 pts.] Plot the current-voltage curve between terminals 1 and 2 over the range indicated on the graph below. Use the mask layout to determine the number of squares of each resistor; there is no need to account for the spreading of dopants during annealing.



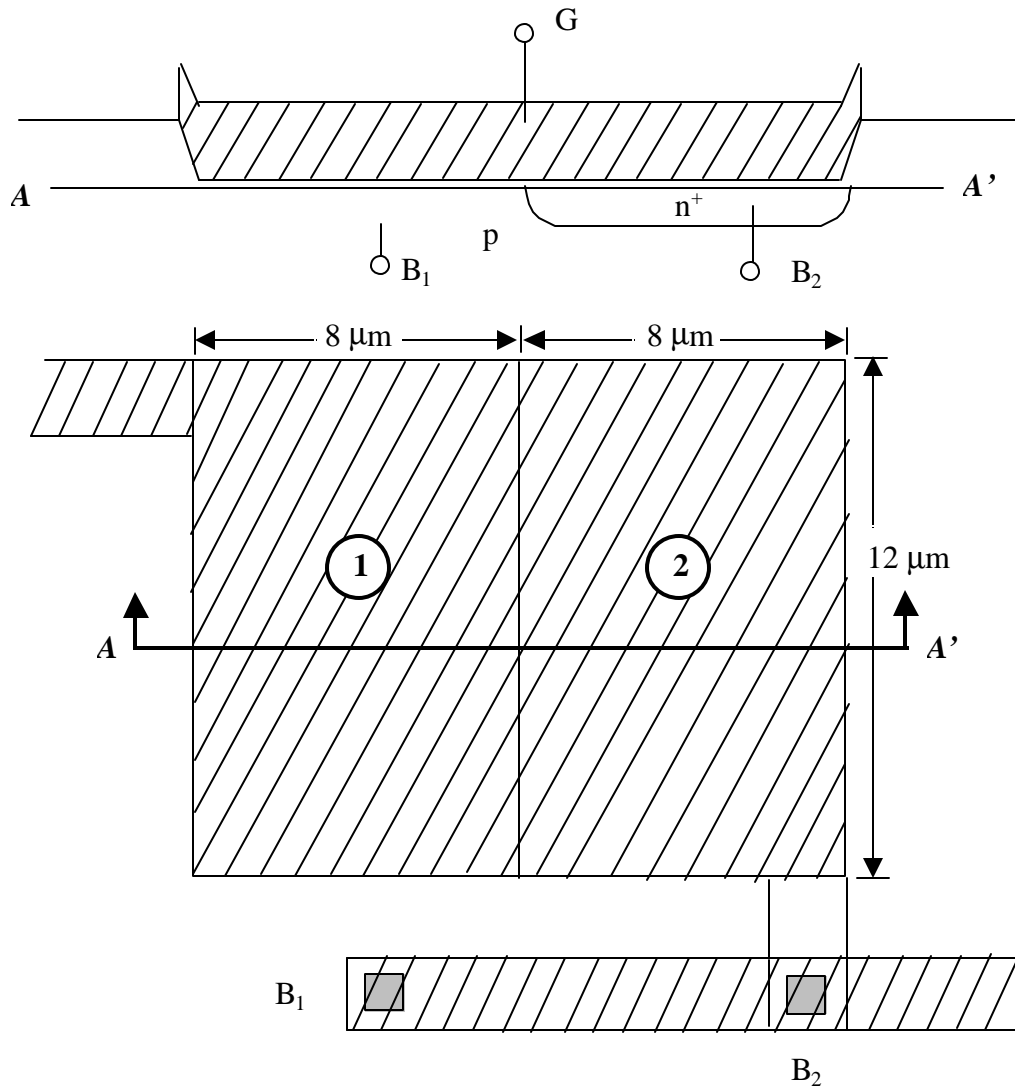
(e) [3 pts.] The total voltage between terminals 1 and 2 is:

$$v_{12}(t) = V_{DC} + v_{ac} \cos(\omega t)$$

with  $V_{DC} = 7.5 \text{ V}$  and  $v_{ac} = 5 \text{ mV}$ . What is the small-signal component of the current between terminals 1 and 2?

$i_{12}(t) =$
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2. MOS charge-storage element [17 pts.]



The MOS structure shown in cross section and top view above has a metal gate and two bottom electrodes, B<sub>1</sub> (p substrate) and B<sub>2</sub> (n<sup>+</sup> layer). The bottom electrodes are contacted by a metal line and shorted together, as indicated on the top view. The oxide thickness is  $t_{ox} = 11.5 \text{ nm}$  for the MOS structure and the oxide permittivity is  $\epsilon_{ox} = 3.45 \times 10^{-13} \text{ F/cm}$ .

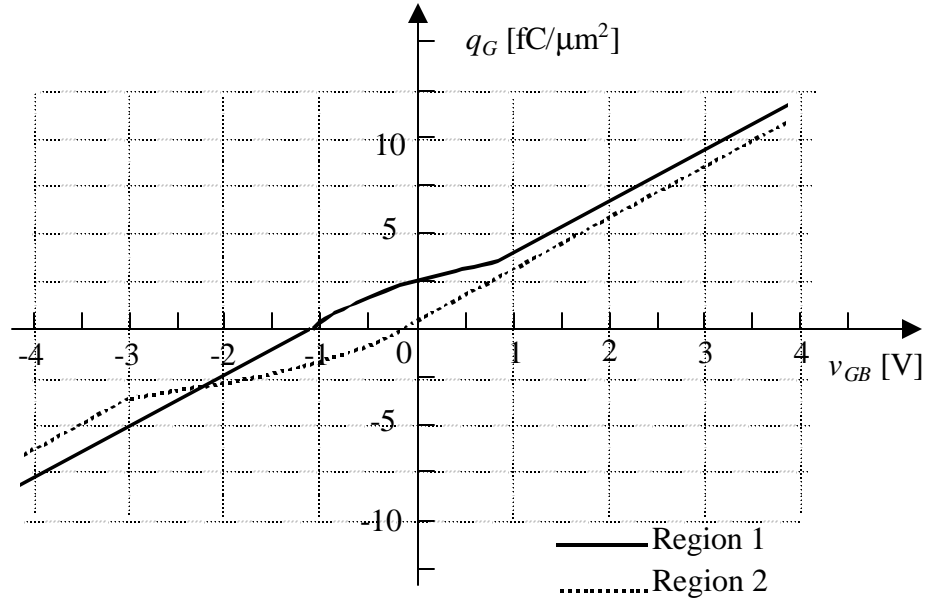
In region 1, the p-type substrate is the bottom electrode and the MOS parameters are:

$$V_{FB} = -1.2 \text{ V}, V_{Tn} = 0.8 \text{ V}$$

In region 2, the n<sup>+</sup> layer is the bottom electrode and the MOS parameters are:

$$V_{FB} = -0.2 \text{ V}, V_{Tp} = -3 \text{ V}$$

The charge storage curves for the two regions are provided on the graphs below of gate charge per unit area versus the gate-bottom electrode potential,  $v_{GB}$ . Since  $B_1 = B_2$ , we use “B” to represent the potential of the bottom electrode for each region.



- (a) [4 pts.] For  $v_{GB} = 1$  V, find the total charge on the gate (units: femtoCoulombs =  $10^{-15}$  C).

$q_{G,Total} =$	fC
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- (b) [4 pts.] For  $v_{GB} = -1.5$  V, identify the *substrate* charge in regions 1 and 2 by circling the correct description(s). Note: the correct answer may have more than one item circled.

Region 1.   ionized acceptors   accumulated holes   inversion-layer electrons

Region 2.   ionized donors   accumulated electrons   inversion-layer holes

(c) [4 pts.] For  $v_{GB} = +1.5$  V, identify the substrate charge in regions 1 and 2 by circling the correct description(s). Note: the correct answer may have more than one item circled.

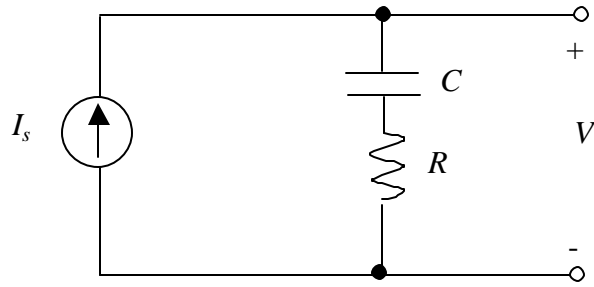
Region 1.   ionized acceptors   accumulated holes   inversion-layer electrons

Region 2.   ionized donors   accumulated electrons   inversion-layer holes

(d) [3 pts.] If we apply a voltage  $v_{GB}(t) = 0$  V +  $v_{gb}\cos(\omega t)$ , where  $v_{gb}=5$  mV and  $\omega = 2\pi(10^6)$  rad/s, find the current  $i_{gb}(t)$  into the gate terminal in nA from the charge-storage curves.

(e) [2 pts.] The maximum capacitance of the MOS structure is  $C_{max}$ . If the DC component of  $v_{GB}$  is 1.5 V, what is the maximum amplitude of its small-signal component  $v_{gb}(t)$  for which the current remains exactly proportional to  $C_{max}$ .

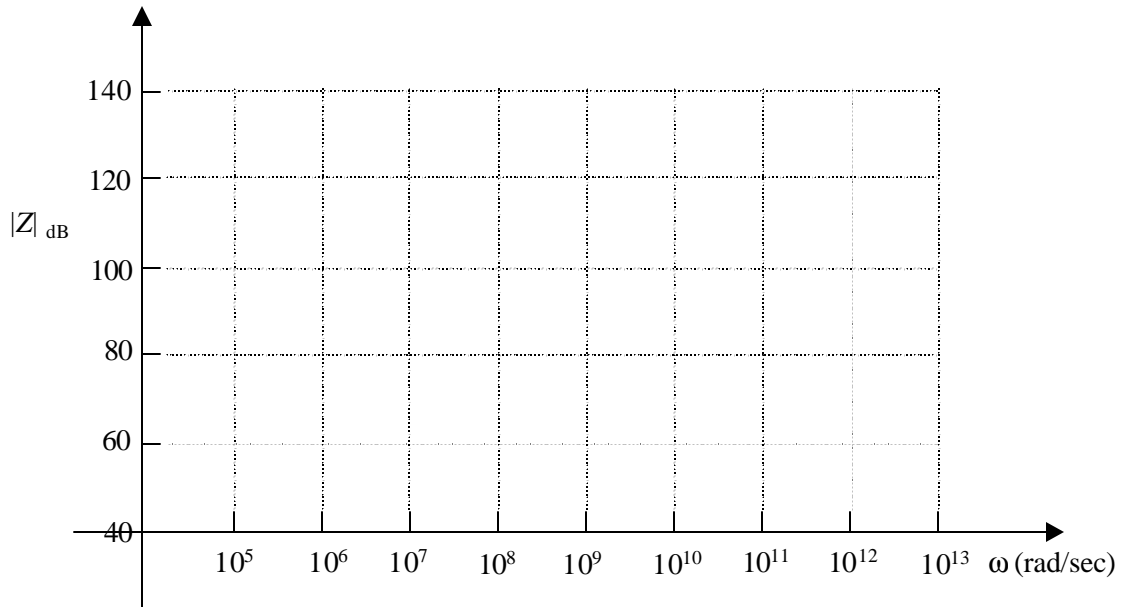
3. Impedance measurements [16 pts.]



The capacitance  $C = 1 \text{ pF}$  and the resistance  $R = 1000 \text{ } \Omega$ .

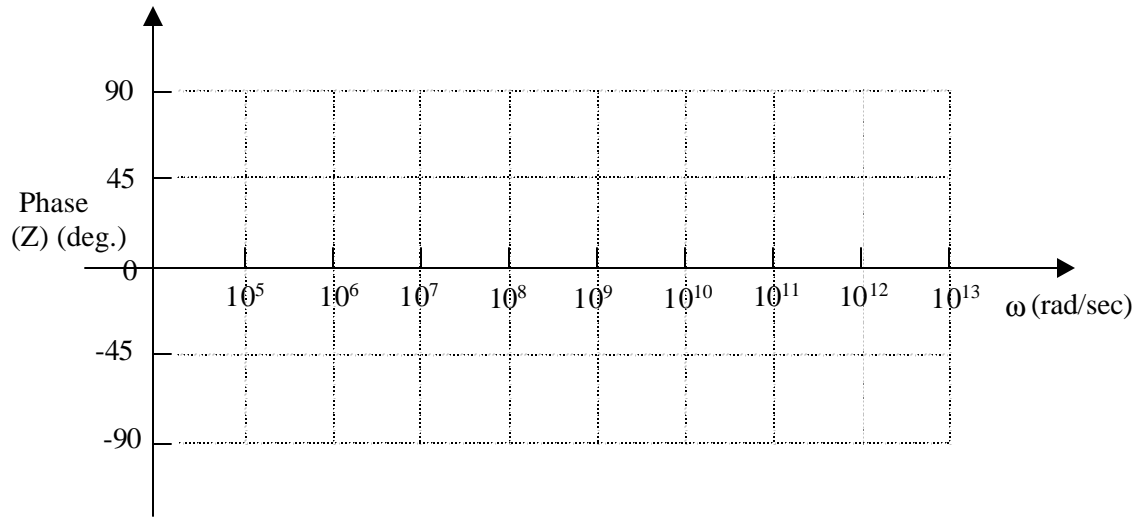
(a) [4 pts.] Find an expression for the impedance  $Z = V/I_s$ . Your result should contain the term  $(1 + j \omega\tau)$ .

(b) [4 pts.] Sketch the magnitude Bode plot for the impedance  $Z$  (units:  $20 \log_{10}(\Omega)$ ) on the graph below using straight-line approximations.

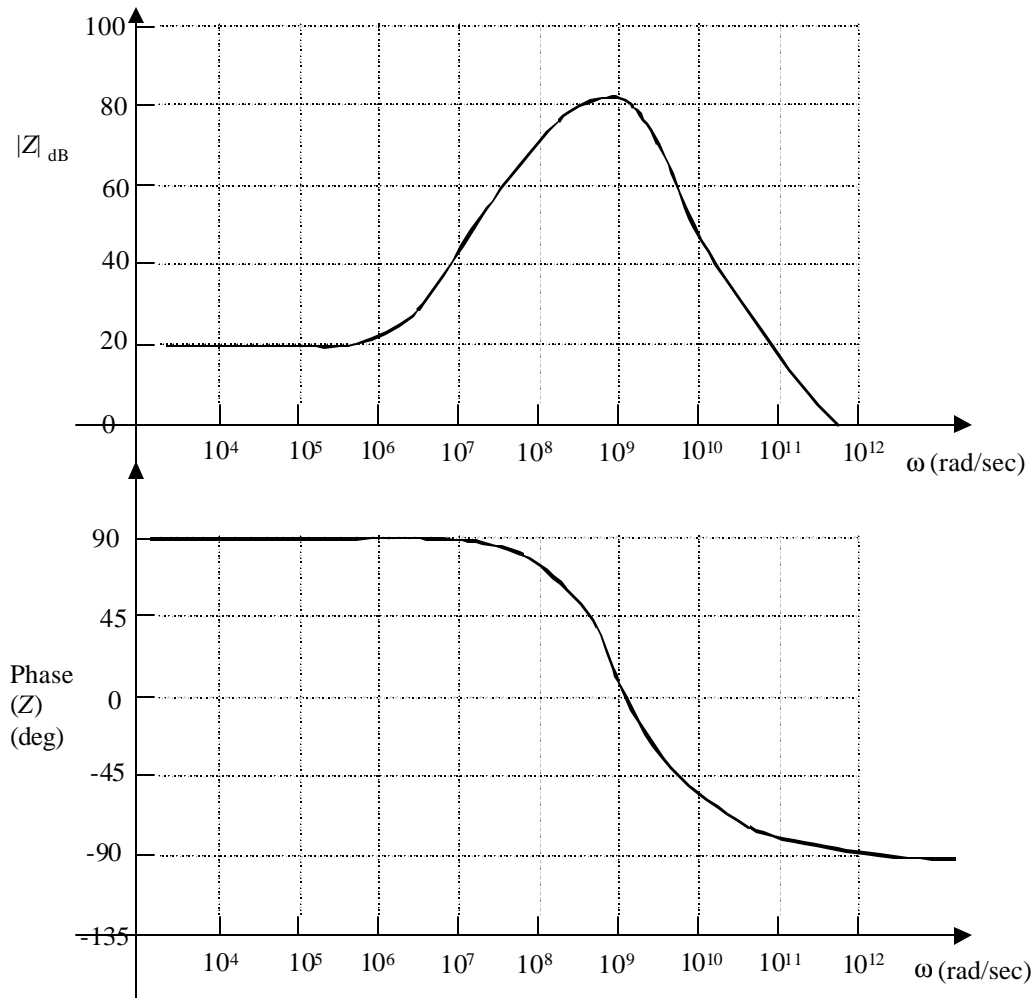




(c) [4 pts.] Sketch the phase of the impedance  $Z$  (units: degrees) on the graph below using straight-line approximations.



(d) [4 pts.] You hook up another two-terminal circuit and measure its impedance. The Bode plots of the magnitude and the phase of  $Z$  are plotted below.



If a phasor current  $I_s = (2.5\text{mA})e^{j0^\circ}$  at a frequency of  $10^8$  rad/sec, what is the voltage waveform  $v(t)$  based on the information in the Bode plots?