

(Clancy)
1999

Solutions and grading standards for exam 2

Information

Students took the exam. Scores ranged from 1 to 20, with a median of 10 and an average of 10.6. There were 42 scores between 16 and 20, 82 between 11 and 15.5, 42 between 6 and 10.5, and 42 between 1 and 5.5. (Were you to receive a grade of 16 on your midterm exams, 48 on the final exam, plus good grades on homework and lab, you would receive an A-; similarly, a test grade of 11 may be projected to a B-.)

There were four versions of the exam, A, B, C, and D. (The version indicator appears at the bottom of the first page.) Versions A and C were identical except for the order of the problems. Versions B and D were also identical except for the order of the problems.

If you think we made a mistake in grading your exam, describe the mistake in writing and send the description with the exam to your lab t.a. or to Mike Clancy. We will consider the entire exam.

Solutions and grading standards for versions A and B

Problem 0 (1 point)

If you earned some credit on a problem and did not put your name on the page, you lost 1/2 point. If you did not indicate your lab section and t.a., you lost 1/2 point. If you did not put the names of your neighbors on the front page, you lost 1/2 point.

Problem 1 (3 points on version A, 4 points on version B)

Two versions of this problem were based on analysis activities you did in lab assignment 7 and homework assignment 7.

Version A, this problem involved analysis of a hashCode function for use with a hash table of size 10000 storing intervals whose endpoints were between -100 and 100.

```
public int hashCode ( ) {
    return left * right;
```

The function does not spread out collisions evenly. 201 nonempty intervals hash to 0; 201 intervals hash to composite table positions; only two intervals hash to each prime number between -100 and 100; no intervals hash to prime numbers between 10000 or to their negative counterparts. (14,188 values between -10,000 and 10,000 cannot be returned by the hashCode function.)

Points for this problem were awarded as follows:

- 1 point for saying that the function was bad;
- 1 point for noting *either* that composite table positions had a lot of collisions or that prime table positions had very few;
- 1 point for noting *both* the above, or for noting one of them and making it clear that there were table cells that have a lot of collisions as well as cells that have

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Saying only that some positions got a lot of collisions was insufficient since a hash function might distribute the remaining keys evenly across the cells.

The hashCode function returns negative values for intervals that overflowed. Some students thought that negative return values would cause trouble with java.util.Hashtable objects map the complete range of integers into a hash table index values. No deduction was made for this error, however.

Version B also involved analyzing a hash function, this one applied to words.

```
public int hashCode ( ) {
    int h = 0;
    for (int k=0; k<s.length(); k++) {
        h = 2 * (h + s.charAt (k));
    }
    return h;
```

This function returns an even integer value for every word. Thus for half the table cells will be empty. For large table sizes, the same sort of problem noticed in homework assignment 7, exercise 4, would appear because of the distribution of English words, as suggested in the table below. (Few students gave this answer.)

word length	maximum hashCode value	maximum hashCode value
3	1358	1708
4	2910	3660
5	6014	7564
6	12222	15372
7	24638	30988
8	49470	62220
9	99134	124664

(Hardly anyone gave this answer.)

This problem was worth 4 points. We awarded 1 point for each correct size and 1 point for a correct corresponding reason, except that we awarded 2 points for two sets of table sizes for which the reason was the same (table sizes divisible by 10 and table sizes divisible by 4). We also gave 2 points for "small table sizes because they produce a lot of collisions". The answer "small table sizes because they waste a lot of space" only received 1 point unless the space was explained in terms of uneven distribution of words.

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Problem 2 (6 points on version A, 7 points on version B)

This problem was derived from work you did in lab assignment 4, homework assignment 4 (version A), lab assignment 5, homework 5, and project 2 (version B). This problem is problem 3 on versions C and D.

Version A involved analyzing a Vector version of the interval combining function from homework 4:

```
public void combine ( ) {
    for (int k=0; k<myIntervals.size()-1; k++) {
        Interval current = (Interval) myIntervals.elementAt (k);
        Interval next = (Interval) myIntervals.elementAt (k+1);
        if (current.overlaps (next)) {
            myIntervals.setElementAt (current.extendThrough (next), k);
            myIntervals.removeElementAt (k+1);
        }
    }
}
```

Version B involved analyzing a Vector version of the function that deletes squares from project 2:

```
public void deleteAll (int x, int y) {
    for (int k=0; k<mySquares.size(); k++) {
        if (((Square) mySquares.elementAt (k)).contains (x, y)) {
            mySquares.removeElementAt (k);
        }
    }
}
```

Both functions had a bug resulting from the rearrangement of index values resulting from deleting a Vector element. When element k is deleted, its successor is the new element k ; since the loop variable is incremented each time through the loop, an interval or square that follows one that gets deleted is not examined. Note that the `removeElementAt` method also decreases the vector's size, something that some students apparently didn't know.

Part a was worth 2 points. The answer in version A was that any list with a sequence of three or more overlapping intervals is handled incorrectly; in version B, any list of consecutive squares that contain the point (x,y) is handled incorrectly. 1 point was awarded for a vague but possibly correct answer, an answer that gave only an example, or an answer that explained what was wrong with the code but failed to identify the vectors for which it would perform incorrectly.

Part b was worth 2 points in version A and 1 point in version B. Any of the following answers received full credit:

- Add a statement that decrements k to the if clause;
- Create an else clause that increments k , and then remove the k increment from the for loop header;
- Place the for loop header so as to process the list elements in reverse order;
- Change the for to a while loop that incorporated one of the above modifications.

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A more extensive fix received only half credit (1 point on version A, 2 points on version B). No points were awarded to an incorrect fix, nor to a method that represented "deleted" elements as empty intervals or squares of size zero.

Part c involved comparing timings of the fixed code and the bug. The inefficiency of the `combine` and `deleteAll` methods compared to the version in homework results from deleting list elements from the middle of the list, which requires shifting the elements that follow. The more elements that are deleted, the more code takes to execute. The corrected version of each method does not delete more list elements, and therefore will take more time.

One may observe two features of the listed timings.

- One column's timings are uniformly greater than the other's. The timings correspond to the corrected version. Moreover, the test list makes the corrected version work harder, namely one with a lot of three or more overlapping intervals or one with a lot of consecutive squares.
- Also, the increase in the time is greater than linear in N ; for version A, it is roughly triple when N is increased from 512 to 1024 and from 1024 to 2048. The rate of growth as N increases is itself increasing. This growth is more pronounced on the test list that contains a lot of intervals. On lists with relatively few intervals/squares, both methods will take time proportional to N .

This part was worth 4 points, 1 for identifying which program version was faster, 1 for identifying to which column, 1 for justifying the answer, 1 for identifying the test list as one containing "many overlapping intervals/squares" was sufficient.

A fix to the code that produced linear-time behavior usually also earned 2 points in part c. One could still get 2 out of the 4 points for identifying the bug, however. Some students seemed to think that `combine` or `deleteAll` applied to a list, then to the same list with all deletable elements already removed, clearly not produce the listed figures.

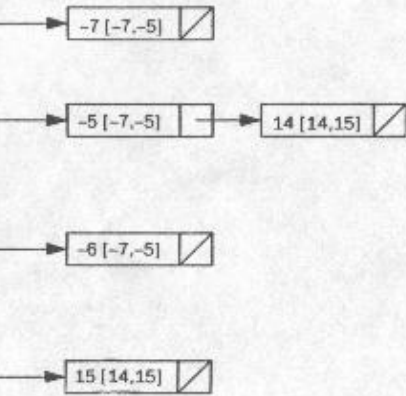
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3 (8 points)

em was derived from homework assignment 4, from hashing exercises in
ment 7 and homework assignment 7, and from the use you made of hash-
network assignment 8. (It was problem 2 on versions C and D.)

as to store nonoverlapping intervals in such a way that they could be
quickly given any integer in the interval. That means that the interval
useful as a key value; instead, the integers in the interval should be used
d the interval stored multiple times in the table. Here's a diagram of how
-7,-5] and [14,15] might be stored in a chained table:



an interval into the table is done as follows:

```

c void insert (Interval intvl) {
  for (int k=intvl.left; k<=intvl.right; k++) {
    myIntervals.put (new Integer (k), intvl);
  }
}
  
```

to retrieve an interval:

```

c Interval intervalContaining (int x) {
  return (Interval) myIntervals.get (new Integer (x));
}
  
```

insertion behavior results from long intervals (note that insertion can
one at the start of a chain, and thus any particular integer can be
constant time). Worst-case retrieval results from lots of collisions.

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Large intervals, incidentally, are not specifically a cause for concern
lem specified that only *nonoverlapping intervals* would be stored. Any
might fill up.

Part a was worth 4 points. You received at least 1 point for indicating
intervals containing only a single element rather than entire intervals
hashed. A second point was earned for any solution that applied the h
all the integers in each interval stored. The third and fourth points w
solutions that stored an interval (actually a reference to an interval)
ger key, and that did not limit the ability of the java.util.hashTable obj
the table if it filled up. A diagram inconsistent with the accompanying
lost 1 point, except that no points were deducted for a diagram that sh
integers mapped to adjacent hash table chains. (A reasonable hash fu
probably not map adjacent integers anywhere near each other.) Many
devised inappropriate hash functions in an attempt to make the exam
collide, thereby losing 2 points; we had hoped to avoid this by includin
"assume for the purposes of illustration".

Part b was worth 2 points. You needed to earn at least 2 points on par
points on this part. Solutions that failed to cast the value retrieved fr
that failed to convert an int into an Integer (or that made both errors)
Solutions that searched or inserted into a chain rather than letting th
method do it lost 1 point.

In part c, we attempted to evaluate your solution to part b; no solution
part b meant no points on part c. Giving any expression involving "N"
what N was earned 0 points out of the 2 for this part. (N could be the l
or the number of intervals in the abstract collection, or the number of
stored in the actual collection.) You had to say something about the "lo
or the "maximum" number of collisions (since the problem asked for v
behavior) for full credit. 1 point was deducted for omitting a mention
in this way.