

UNIVERSITY OF CALIFORNIA  
 Department of Electrical Engineering  
 and Computer Sciences  
 Computer Science Division

Prof. R. Fateman

Fall, 2001

**Solutions: CS 164 Midterm 1: September 26, 2001, 9:00AM**

1. [20 points] Here is a table describing an automaton with 2 states. The start state is S.
- a. Draw a diagram of the automaton in the space to the right of the table. I'm not good at drawing in tex. The expected solution has two states, S and T. From S to itself is an arc labeled 0,1. From S to T is an arc labeled 0. From T to T is an arc labeled 0. T is a final state, S has an incoming arc as the initial state.
  - b. Write down a simple regular expression that describes the same language that is recognized by this automaton.  
 $(0 \mid 1)^*0$  is the simplest solution.
  - c. In the space below, draw a DFA that accepts the same language. Use as few states as possible.  
 Two states, the same as above except that instead of an arc from S to S labeled 0,1 there is an arc from T to S labeled 1.
  - d. Write a context free grammar  $G_0$  that describes the same language.  
 Here's one.

$X \rightarrow T0$   
 $T \rightarrow 0T \mid 1T \mid \epsilon$

2. [5 points] Write down a precise definition of  $L(G)$  the language generated by any context free grammar  $G$ .

We expect something like

$L(G) = \{a_1 a_2 \dots a_n \mid a_i \text{ is in terminals}(G), S \Rightarrow^* a_1 a_2 \dots a_n, S \text{ is start}(G)\}$   
 Or in English.. a set of all strings of terminal symbols derived from the start symbol S using rules of G.

State	Transitions	Final State?
	0 1	
S	S,T S	
T	T	yes

3. [6 points] Suppose grammar  $G1$  has only one rule rewriting  $X$ , namely  $X \rightarrow YZW$
- If we know that  $a \in \text{First}(Y)$ , what can you conclude about  $\text{First}(X)$ ?  
A is in  $\text{First}(x)$
  - Under what condition is  $\text{First}(W) \subset \text{First}(X)$ ?  
if  $\epsilon \in \text{First}(Y)$  and  $\epsilon \in \text{First}(Z)$ .
  - Under what condition is  $\epsilon \in \text{First}(X)$ ?  
The condition above with  $\epsilon \in \text{First}(W)$  also.

4. [5 points] Here are the rules for a grammar  $G2$  with start symbol  $S$

$$S \rightarrow aS$$

$$S \rightarrow b$$

Complete writing a recursive descent parsing program `parse` that returns `yes`, given a lisp list that constitutes a sentence in  $L(G2)$ . We give you two useful parts already.

```
(defun parse (tokens)(s)(if (empty tokens) "yes"))

(defun eat(h) (cond((equal h (car tokens))(pop tokens))
                    (t (error "stuck at ~s" tokens))))
;; sample test: (parse '(a a b))

;; answer
(defun s()(case (car tokens)
              (a (eat 'a)(s))
              (b (eat 'b) t)))
```

5. [10 points] What is the result of running your Tiger lexical analysis program `fs1` on a file containing this material:

```
if then loop else23 >>>= 45
"hello /* world" iconst */
```

Run it to see the answer. It starts with `((if (1 . 2)) (then then ...) ...)`

6. [12 points]  
On the next page is an LL(1) Parsing Table for a grammar  $G3$  with start symbol  $E$ .
- What are the rules of the grammar  $G3$ ?

```
E -> TX
T -> iY | oEc
X-> pE | epsilon
Y-> mT | epsilon
\begin{verbatim}
```

	i	m	p	o	c	\$
E	TX			TX		
X			pE		ε	ε
T	iY			oEc		
Y		mT	ε		ε	ε

b. What are the terminal symbols of  $G_3$ ?

i o c m p and maybe \$

c. Trace each stack configuration in the parsing of the input string  $\{\texttt{o i c}\}$ . We have given you the first stack contents:

`\begin{verbatim}`

step    stack                    input

1.        E \$                    o i c \$
2.        TX\$
3.        oEcX\$
4.        EcX\$
5.        TXcX\$
6.        iYXcX\$
7.        YXcX\$
8.        XcX\$
9.        cX\$
10.       X\$
11.       \$

Note that this grammar, with the substitutions of  $m=*$ ,  $p=+$ ,  $o=($  and  $c=)$  should be familiar to you.

7. [2 points]

a. Describe any unusual piece of clothing worn on Monday Sept. 24, by Prof. Fateman for the first 8 minutes of CS164 lecture.

You had to be there to see it.

b. How many CS164 lectures were delivered without the use of the video projector?

Ditto.